

[arXiv:1211.1316](#) **Bounds for the Multiplicity of Gorenstein algebras.** Sabine El [Khoury](#), Manoj [Kummini](#), Hema [Srinivasan](#). [math.AC](#).  
An application of Boij-Soederberg Theory.

[arXiv:1210.8069](#) **Betti diagrams from graphs.** Alexander [Engström](#), Matthew T. [Stamps](#). [math.CO](#) ([math.AC](#)).  
Application of Boij-Soederberg theory to the edge ideals of graphs.

[arXiv:1207.5467](#) **Asymptotics of random Betti tables.** Lawrence [Ein](#), Daniel [Erman](#), Robert [Lazarsfeld](#). [math.AG](#) ([math.AC](#)).  
--A conjecture based on Boij-Soederberg numerics about the resolutions of high degree embeddings of projective varieties.

[arXiv:1205.0449](#) **Categorified duality in Boij-Söderberg Theory and invariants of free complexes.** David [Eisenbud](#), Daniel [Erman](#). [math.AC](#) ([math.AG](#)).  
--A basic reinterpretation of the Eisenbud-Schreyer duality theory leading to substantial enlargement of the applicability of this idea (such as decompositions of complexes with homology, and duality for multigraded resolutions...)

[arXiv:1203.6515](#) **Combinatorial Interpretations of some Boij-Söderberg Decompositions.** Uwe [Nagel](#), Stephen [Sturgeon](#). [math.AC](#) ([math.CO](#)).  
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[arXiv:1109.5198](#) **The cone of Betti diagrams over a hypersurface ring of low embedding dimension.** Christine [Berkesch](#), Jesse [Burke](#), Daniel [Erman](#), Courtney [Gibbons](#). Mittag-Leffler-2011spring. [math.AC](#).  
--An exploration of the cone of Betti tables in the simplest case with infinite resolutions.

[arXiv:1106.0381](#) **Boij-Söderberg theory: Introduction and survey.** Gunnar [Floystad](#). *Progress in Commutative Algebra 1*, Combinatorics and homology, (C. Francisco et.al. eds.), Proceedings in mathematics, du Gruyter, 2012, pp. 1-54. [math.AC](#).  
--An extensive exposition of Boij-Soederberg theory. Unfortunately it was written too early to make use of the categorified duality of Eisenbud-Erman.

[arXiv:1102.3559](#) **Betti Numbers of Syzygies and Cohomology of Coherent Sheaves.** David [Eisenbud](#), Frank-Olaf [Schreyer](#). *Proceedings of the ICM, Hyderabad2010*, vol. 2, 586--602. [math.AG](#) ([math.AC](#)).  
--An exposition and some simplified proofs, based on Schreyer's ICM lecture.

[arXiv:1109.4591](#) **The Banks of the Cohomology River.** David [Eisenbud](#), [math.AG](#).

--An application of Boij-Soederberg ideas (though not directly the theory) to the question: given the cohomology tables of sheaves E,F, what can be said about the cohomology of the tensor product? Introduces higher regularity indices and their expression in terms of linear monads.

[arXiv:1101.4604](#) **Tensor complexes: Multilinear free resolutions constructed from higher tensors.** Christine [Berkesch](#), Daniel [Erman](#), Manoj [Kummini](#), Steven V [Sam](#). Mittag-Leffler-2011spring. [math.AC](#) ([math.AG](#)).

--Extends the Eisenbud-Schreyer construction of pure resolutions by introducing coefficients, obtaining a much larger family of complexes that generalizes, in particular, the family defined by Buchsbaum and Eisenbud that includes the Eagon-Northcott and Buchsbaum-Rim complexes.

[arXiv:1010.2663](#) **Poset structures in Boij-Söderberg theory.** Christine [Berkesch](#), Daniel [Erman](#), Manoj [Kummini](#), Steven V [Sam](#). Mittag-Leffler-2011spring. *Int. Math. Res. Not. IMRN* (2012), no. 22, 5132-5160. [math.AC](#) ([math.AG](#)).

--An interpretation of the poset structure of degree sequences in terms of homomorphisms of modules; part of a program to "explain" some of the consequences of Boij-Soederberg theory in module or sheaf-theoretic terms.

[arXiv:1006.2026](#) **The structure of the Boij-Söderberg posets.** David [Cook II](#). *Proceedings of the American Mathematical Society* 139 (2011), no. 6, 2009-2015. [math.CO](#).

--A combinatorial analysis of the cone of Betti tables from the point of view of the lattice of degree sequences in a given interval, generalizing

facts about the Bruhat order to the case of degree sequences of differing lengths.

[arXiv:1001.3238](#) **The cone of Betti diagrams of bigraded artinian modules of codimension two.** Mats [Boij](#), Gunnar [Floystad](#). [math.AC](#).  
--An extension of the theory beyond the singly graded case.

[arXiv:1001.0585](#) **Filtering free resolutions.** David [Eisenbud](#), Daniel [Erman](#), Frank-Olaf [Schreyer](#). [math.AC](#) ([math.AG](#)).  
Gives sufficient conditions under which the Boij-Soederberg decomposition of a Betti table is reflected in the decomposition of the resolutions. Uses this to compute the semigroup of Betti tables in the case of modules over  $k[x,y,z]$  generated in degree  $\geq 0$  and having regularity  $\leq 1$ . Part of a program to "explain" some of the consequences of Boij-Soederberg theory in module or sheaf-theoretic terms.

[arXiv:0907.4505](#) **Pieri resolutions for classical groups.** Steven V [Sam](#), Jerzy [Weyman](#). *J. Algebra* 329 (2011), 222-259. [math.AC](#) ([math.CO](#) [math.RT](#)).  
--Reproves and extends the constructions of pure resolutions in Eisenbud-Floystad-Weyman.

[arXiv:0907.3912](#) **Some algebraic consequences of Green's hyperplane restriction theorems.** Mats [Boij](#), Fabrizio [Zanello](#). *JPA* 214 (2010), no. 7, 1263-1270. [math.AC](#)([math.AG](#)).

[arXiv:0902.0316](#) **A special case of the Buchsbaum-Eisenbud-Horrocks rank conjecture.** Daniel [Erman](#). *Mathematical Research Letters*, 17 (2010), 1079-1089. [math.AC](#) ([math.AG](#)).  
--Applies Boij-Soederberg theory to prove the Buchsbaum-Eisenbud-Horrocks conjecture on the sum of the ranks in a free resolution in a certain range of cases.

[arXiv:0806.4401](#) **The Semigroup of Betti Diagrams.** Daniel [Erman](#). *Algebra and Number Theory*, 3 (2009), 341-365. [math.AC](#) ([math.AG](#)).  
--Proves that the semigroup of Betti tables in a finite interval is finitely generated. Gives generators in the the smallest cases.

[arXiv:0803.1645](#) **Betti numbers of graded modules and the Multiplicity Conjecture in the non-Cohen-Macaulay case.** Mats [Boij](#), Jonas [Soderberg](#). [math.AC](#)([math.AG](#)).

--Treats the non-Cohen-Macaulay case. Extends the original conjectures and proves the extension using the Eisenbud-Schreyer pairings.

[arXiv:0712.1843](#) **Betti Numbers of Graded Modules and Cohomology of Vector Bundles.** David [Eisenbud](#), Frank-Olaf [Schreyer](#). [math.AC](#) ([math.AG](#)).

--proves Boij-Soederberg conjectures, and the analogous conjectures for the cone of cohomology tables by introducing a family of pairings between these cones. Proves existence of pure resolutions and supernatural vector bundles in all characteristics.

[arXiv:0709.1529](#) **The Existence of Pure Free Resolutions.** David [Eisenbud](#), Gunnar [Floystad](#), Jerzy [Weyman](#). *Annales de l'institut Fourier*, 61 (2011), no. 3, p. 905-926. [math.AC](#) ([math.RT](#)).

--proves existence of equivariant pure resolutions in characteristic 0.

[math/0611081](#) **Graded Betti numbers of Cohen-Macaulay modules and the Multiplicity conjecture.** Mats [Boij](#), Jonas [Söderberg](#). [math.AC](#).

--The paper with the conjectures for the cone of Betti tables of Cohen-Macaulay modules that led to the theory.

J. Herzog and H. Srinivasan. Bounds for Multiplicities. *Trans. Am. Math. Soc.* (1998) 2879–2902.

--The "Multiplicity Conjecture" of Herzog-Huneke-Srinivasan that started the whole process.

J. Herzog and M. K\"uhl. On the betti numbers of finite pure and linear resolutions. *Comm. in Alg.* 12 (13) (1984) 1627–1646.

--A basic result about pure resolutions.