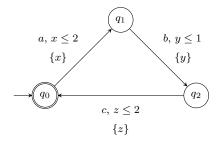
TMAT Tutorial 1

- 1. Give a timed automaton over $\Sigma = \{a, b\}$ that accepts all timed words.
- 2. Let $\mathcal{A} = (\{q\}, \{a, b\}, \{x\}, T, \{q\}, \{q\}))$ be a timed automaton with a single state q and a single clock x. Note that q is also an accepting state. Let T be the set of transitions. Give an instance of T that makes \mathcal{A} reject at least one timed word.
- 3. What is the timed word accepted by the following accepting run of some timed automaton with two clocks x and y?

4. Let \mathcal{B} be the following timed automaton:



Consider the timed word s = (abcabc, 0.5, 1, 1.5, 1.8, 1.9, 3).

- a) Does \mathcal{B} accept s? If so, write down the accepting run of \mathcal{B} on s.
- b) For a timed word (w,τ) we define the *time span* of (w,τ) to be the time at which the last letter occurs, i.e., if |w| = n, then time span of (w,τ) is τ_n .

For every $k \in \mathbb{N}$, give a timed word in $\mathcal{L}(\mathcal{B})$ that has length greater than k and whose time span is lesser than 1.

- 5. Give a timed automaton for the timed language of all words in $(a + b)^*$ such that there exist two a-s which are at distance 1 apart and there exist two b-s which are at distance 2 apart.
- 6. Let $\Sigma = \{a, b\}$. Construct timed automata for the following languages:
 - (a) $\{(w,\tau) \mid \text{ there is an } a \text{ at some time } t \text{ and no action occurs at time } t+1 \}$
 - (b) $\{(w,\tau) \mid \text{ all } a$'s occur before time 1 and no two a's happen at the same time $\}$
 - (c) $\{(a^k, \tau) \mid k \ge 1, \tau_1 = 1, \text{ and } \tau_{i+2} \tau_i \le 1 \text{ for all } 1 \le i \le k-2\}$