Programming in Haskell

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- To describe a collection of values
 - [1,2,3,1] is a list of Int
 - [True,False,True] is a list of Bool
- Elements of a list must be of a uniform type
 - Cannot write [1,2,True] or [3,'a']



- List with values of type T has type [T]
 - [1,2,3,1] :: [Int]
 - [True,False,True] :: [Bool]
 - [] denotes the empty list, for all types
- Lists can be nested
- [[3,2], [], [7,7,7]] is of type [[Int]]

Internal representation

- To build a list, add one element at a time to the front (left)
 - Operator to append an element is :
 - 1:[2,3] ⇒ [1,2,3]
- All Haskell lists are built this way, starting with []
 - [1,2,3] is actually 1:(2:(3:[]))
 - : is right associative, so 1:2:3:[] is 1:(2:(3:[]))
- 1:[2,3] == 1:2:3:[], 1:2:[3] == [1,2,3], ... all return True

Decomposing lists

- Functions head and tail
 - head (x:xs) ⇒ x
 - tail (x:xs) ⇒ xs
 - Both undefined for []
 - head returns a value, tail returns a list

Defining functions on lists

- Recall inductive definition of numeric functions
 - Base case is f 0
 - Define f (n+1) in terms of n+1 and f n
- For lists, induction on list structure
 - Base case is []
 - Define f (x:xs) in terms of x and f xs

Example: length

• Length of [] is 0

• Length of (x:xs) is 1 more than length of xs

```
• mylength :: [Int] -> Int
mylength [] = 0
mylength l = 1 + mylength (tail l)
```

Pattern matching

- A nonempty list decomposes uniquely as x:xs
 - Pattern matching implicitly separates head, tail
 - Empty list will not match this pattern
 - Note the bracketing: (x:xs)

```
• mylength :: [Int] -> Int
mylength [] = 0
mylength (x:xs) = 1 + mylength xs
```

Example: sum of values

• Sum of [] is 0

• Sum of (x:xs) is x plus sum of xs

```
• mysum :: [Int] -> Int
mysum [] = 0
mysum (x:xs) = x + mysum xs
```



- Positions in a list are numbered 0 to n-1
 - l!!j is the value at position j
 - Accessing value **j** takes time proportional to **j**
 - Need to "peel off" j applications of : operator
 - Contrast with arrays, which support random access

- [m..n] ⇒ [m, m+1, ..., n]
 - Empty list if n < m

• Skipping values (arithmetic progressions)

• $[1,3..8] \Rightarrow [1,3,5,7]$ $[2,5..19] \Rightarrow [2,5,8,11,14,17]$

• Descending order

• $[8,7..5] \Rightarrow [8,7,6,5]$ $[12,8..-9] \Rightarrow [12,8,4,0,-4,-8]$

Example: appendright

- Add a value to the end of the list
 - An empty list becomes a one element list
 - For a nonempty list, recursively append to the tail of the list

```
    appendr :: Int -> [Int] -> [Int]
appendr x [] = [x]
appendr x (y:ys) = y:(appendr x ys)
```

Example: attach

- Attach two lists to form a single list
 - attach [3,2] [4,6,7] ⇒ [3,2,4,6,7]

Induction on the first argument

• attach :: [Int] -> [Int] -> [Int] attach [] l = l attach (x:xs) l = x:(attach xs l)

• Built in operator ++

• [3,2] ++ [4,6,7] ⇒ [3,2,4,6,7]

Example: reverse

- Remove the head
- Recursively reverse the tail
- Attach the head at the end

```
• reverse ::[Int] -> [Int]
reverse [] = []
reverse (x:xs) = (reverse xs) ++ [x]
```

Example: is sorted

- Check if a list of integers is in ascending order
- Any list with less than two elements is OK

```
    ascending :: [Int] -> Bool
ascending [] = True
ascending [x] = True
ascending (x:y:ys) = (x <= y) &&
ascending (y:ys)
```

• Note the two level pattern

Example: alternating

- Check if a list of integers is alternating
 - Values should strictly increase and decrease at alternate positions
- Alternating list can start in increasing order (updown) or decreasing order (downup)
 - tail of a downup list is updown
 - tail of an updown list is downup

Example: alternating...

```
• alternating :: [Int] -> Bool
alternating l = (updown l) || (downup l)
```

```
updown :: [Int] -> Bool
updown [] = True
updown [x] = True
updown (x:y:ys) = (x < y) && (downup (y:ys))</li>
downup:: [Int] -> Bool
downup [] = True
downup [x] = True
downup (x:y:ys) = (x > y) && (updown (y:ys))
```

Built in functions on lists

- head, tail, length, sum, reverse, ...
- init l, returns all but the last element

init [1,2,3] ⇒ [1,2]
 init [2] ⇒ []

- last l, returns the last element in l
 - last [1,2,3] ⇒ 3 last [2] ⇒ 2

Built in functions on lists...

- take n l, returns first n values in l
- drop n l, leaves first n values in l
 - Do the "obvious" thing for bad values of **n**
 - l == (take n l) ++ (drop n l), always

Built in functions on lists...

• Defining take



- Functions on lists are typically defined by induction on the structure
- Point to ponder
 - Is there a difference in how length works for [Int], [Float],
 [Bool], ...?
 - Can we assign a more generic type to such functions?