

Programming in Haskell

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LECTURE 5

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S P SURESH

CHENNAI MATHEMATICAL INSTITUTE

The datatype Char

- * Values are written with single quotes
 - * 'a', '3', '%', '#', ...
- * Character symbols stored in a table (e.g. ASCII)
 - * Functions `ord` and `chr` connect characters and table
 - * Inverses: `c == chr (ord c)`, `j == ord (chr j)`
 - * Note: `import Data.Char` to use `ord` and `chr`

Example: capitalize

- * Function to convert lower case to upper case
- * Brute force, enumerate all cases

```
capitalize :: Char -> Char
capitalize 'a' = 'A'
capitalize 'b' = 'B'
...
capitalize 'z' = 'Z'
capitalize ch  = ch
```

Example: capitalize ...

- * Can assume that 'a', ..., 'z' and 'A', ..., 'Z' and '0', ..., '9' each have consecutive `ord` values
- * A more intelligent solution

```
capitalize :: Char -> Char
```

```
capitalize ch
```

```
  | ('a' <= ch && ch <= 'z') =
```

```
    chr (ord ch + (ord 'A' - ord 'a'))
```

```
  | otherwise = ch
```

Strings

- * A string is a sequence of characters
- * In Haskell, `String` is a synonym for `[Char]`
 - * `['h','e','l','l','o'] == "hello"`
 - * `"" == []`
- * Usual list functions can be used on `String`
 - * `length`, `reverse`, ...

Example: occurs

- * Search for a character in a string
- * `occurs c s` returns `True` if `c` is found in `s`

```
occurs :: Char -> String -> Bool
occurs c "" = False
occurs c (x:xs)
  | c == x    = True
  | otherwise = occurs c xs
```

Example: touppercase

- * Convert an entire string to uppercase
- * Apply `capitalize` to each character

```
touppercase :: String -> String
touppercase ""      = ""
touppercase (c:cs) = (capitalize c):
                    (touppercase cs)
```

- * Apply `f` to each element in a list—will come back to this later

Example: position

- * `position c s`: first position in `s` where `c` occurs

- * Return `length s` if no occurrence of `c` in `s`

- * `position 'a' "battle axe" ⇒ 1`

- * `position 'd' "battle axe" ⇒ 10`

```
position :: Char -> String -> Int
```

```
position c "" = 0
```

```
position c (d:ds)
```

```
  | c == d      = 0
```

```
  | otherwise = 1 + (position c ds)
```


Example: Counting words

- * `wordc`: count the number of words in a string
- * Words separated by white space: ' ', '\t', '\n'

```
whitespace :: Char -> Bool
whitespace ' ' = True
whitespace '\t' = True
whitespace '\n' = True
whitespace _   = False
```

Example: Counting words

- * Count white space in a string?

```
wscount :: String -> Int
wscount "" = 0
wscount (c:cs)
  | whitespace c = 1 + wscount cs
  | otherwise   = wscount cs
```

- * Not enough!

- * Consider "abc d"

Example: Counting words

- * Keep track of whether we are inside a word or outside a word
 - * Outside a word: ignore whitespace, but non-whitespace starts a new word
 - * Inside a word: ignore non-whitespace, but whitespace ends current word
- * Count the number of times a new word starts

Example: Counting words

- * New word starts whenever a non-whitespace follows a whitespace—
insert initial space to catch first character

```
wordcaux :: String -> Int
wordcaux [c] = 0
wordcaux (c:d:ds)
  | (whitespace c) && not (whitespace d) =
    1 + wordcaux (d:ds)
  | otherwise = wordcaux (d:ds)
```

```
wordc :: String -> Int
wordc s = wordcaux (' ':s)
```

Tuples

- * Keep multiple types of data together
 - * Student info: Name, ID, Date of birth

("Abhirup", 2106, "Jan 1, 2000")

- * List of marks in a course

```
[("Sasha",95),  
 ("Becky",95),  
 ("Charlotte",98)]
```

Tuples ..

- * Tuple type (T_1, T_2, \dots, T_n) groups together multiple types
 - * $(3, -21) :: (\text{Int}, \text{Int})$
 - * $(13, \text{True}, 97) :: (\text{Int}, \text{Bool}, \text{Int})$
 - * $([1, 2], 73) :: ([\text{Int}], \text{Int})$

Pattern matching

- * Use tuple structure for pattern matching
- * Sum pairs of integers

```
sumpairs :: (Int,Int) -> Int  
sumpairs (x,y) = x+y
```

- * Sum pairs of integers in a list of pairs

```
sumpairlist :: [(Int,Int)] -> Int  
sumpairlist [] = 0  
sumpairlist (x,y):zs = x + y + sumpairlist zs
```

Example: Marks list

- * List of pairs (Name,Marks) — [(String,Int)]
- * Given a name, find the marks

```
lookup :: String -> [(String,Int)] -> Int
lookup p [] = -1
lookup p ((name,marks):ms)
  | (p == name) = marks
  | otherwise   = lookup p ms
```


Type aliases

- * Tedious to keep writing `[(String,Int)]`
- * Introduce a new name for this type

```
type Marklist = [(String,Int)]
```

- * Then

```
lookup :: String -> Marklist -> Int
```

Type aliases ...

- * A type definition only creates an alias for a type
 - * Both `MarkList` and `[(String,Int)]` are the same type
 - * `String` is a type alias for `[Char]`

Example: Point

* `type Point2D = (Float,Float)`

`distance :: Point2D -> Point2D -> Float`

`distance (x1,y1) (x2,y2) =
 sqrt((x2-x1)*(x2-x1) + (y2-y1)*(y2-y1))`

* `type Point3D = (Float,Float,Float)`

`distance :: Point3D -> Point3D -> Float`

`distance (x1,y1,z1) (x2,y2,z2) =
 sqrt((x2-x1)*(x2-x1) + (y2-y1)*(y2-y1) +
 (z2-z1)*(z2-z1))`

Type aliases are same type

- * Suppose

- * $f :: \text{Float} \rightarrow \text{Float} \rightarrow \text{Point2D}$

- * $g :: (\text{Float}, \text{Float}) \rightarrow (\text{Float}, \text{Float}) \rightarrow \text{Float}$

- * Then

- * $g (f \ x1 \ x2) (f \ y1 \ y2)$ is well typed

- * f produces Point2D that is same as $(\text{Float}, \text{Float})$

Local definitions

- * Let us return to distance

- * `type Point2D = (Float,Float)`

```
distance :: Point2D -> Point2D -> Float
```

```
distance (x1,y1) (x2,y2) =
```

```
    sqrt((x2-x1)*(x2-x1) + (y2-y1)*(y2-y1))
```

- * Introduce `sqr` to simplify expressions

Local definitions

```
* sqr :: Float -> Float  
sqr x = x*x
```

```
type Point2D = (Float,Float)
```

```
distance :: Point2D -> Point2D -> Float  
distance (x1,y1) (x2,y2) =  
    sqrt(sqr (x2-x1) + sqr (y2-y1))
```

* But now, auxiliary function `sqr` is globally available

Local definitions

```
type Point2D = (Float,Float)
```

```
distance :: Point2D -> Point2D -> Float
```

```
distance (x1,y1) (x2,y2) =  
  sqrt(sqr (x2-x1) + sqr (y2-y1))
```

```
where
```

```
sqr :: Float -> Float
```

```
sqr x = x*x
```

- * Definition of `sqr` is now local to `distance`

Local definitions

- * Another motivation

```
type Point2D = (Float,Float)
```

```
distance :: Point2D -> Point2D -> Float
```

```
distance (x1,y1) (x2,y2) =  
    sqrt(xdiff*xdiff + ydiff*ydiff)
```

```
where
```

```
xdiff :: Float
```

```
xdiff = x2 - x1
```

```
ydiff :: Float
```

```
ydiff = y2 - y1
```


Local definition

- * $xdiff * xdiff$ vs $(x2-x1) * (x2-x1)$
- * With $xdiff * xdiff$, $(x2-x1)$ is only computed once
- * In general, ensure that common subexpressions are evaluated only once

Summary

- * Tuples allow different types to come together in a single unit
 - * Pattern matching to extract individual components
- * `type` statement creates type aliases
- * `where` allows local definitions