

NPTEL MOOC, JAN-FEB 2015
Week 2, Module 3

DESIGN AND ANALYSIS OF ALGORITHMS

Selection Sort

MADHAVAN MUKUND, CHENNAI MATHEMATICAL INSTITUTE
<http://www.cmi.ac.in/~madhavan>

Sorting

- * Searching for a value
 - * Unsorted array — linear scan, $O(n)$
 - * Sorted array — binary search, $O(\log n)$
- * Other advantages of sorting
 - * Finding **median** value: midpoint of sorted list
 - * Checking for duplicates
 - * Building a frequency table of values

How to sort?

- * You are a Teaching Assistant for a course
- * The instructor gives you a stack of exam answer papers with marks, ordered randomly
- * Your task is to arrange them in descending order

Strategy 1

- * Scan the entire stack and find the paper with minimum marks
- * Move this paper to a new stack
- * Repeat with remaining papers
 - * Each time, add next minimum mark paper on top of new stack
- * Eventually, new stack is sorted in descending order

Strategy 1 ...

74

32

89

55

21

64

Strategy 1 ...

74

32

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55

~~21~~

64

21

Strategy 1 ...

74

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89

55

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32

Strategy 1 ...

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32

55

Strategy 1 ...

74

~~32~~

89

~~55~~

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21

32

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64

Strategy 1 ...

74	32	89	55	21	64
21	32	55	64	74	

Strategy 1 ...



The diagram illustrates a sequence of numbers arranged in two rows. The top row contains six numbers: 74, 32, 89, 55, 21, and 64. Each of these numbers is crossed out by a red diagonal line. The bottom row contains six numbers: 21, 32, 55, 64, 74, and 89. These numbers are not crossed out.

74	32	89	55	21	64
21	32	55	64	74	89

Strategy 1 ...

Selection Sort

- * **Select** the next element in sorted order
- * Move it into its correct place in the final sorted list

Selection Sort

- * Avoid using a second list
 - * Swap minimum element with value in first position
 - * Swap second minimum element to second position
 - * ...

Selection Sort

74

32

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Selection Sort

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Selection Sort

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Selection Sort

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Selection Sort

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Selection Sort

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Selection Sort

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74

89

Selection Sort

```
SelectionSort(A,n) // Sort A of size n
```

```
for (startpos = 0; startpos < n; startpos++)
```

```
    // Scan segments A[0]..A[n-1], A[1]..A[n-1], ...
```

```
    // Locate position of minimum element in current segment
```

```
    minpos = startpos;
```

```
    for (i = minpos+1; i < n; i++)
```

```
        if (A[i] < A[minpos])
```

```
            minpos = i;
```

```
    // Move minimum element to start of current segment
```

```
    swap(A,startpos,minpos)
```


Analysis of Selection Sort

- * Finding minimum in unsorted segment of length k requires one scan, k steps
- * In each iteration, segment to be scanned reduces by 1
- * $t(n) = n + (n-1) + (n-2) + \dots + 1 = n(n+1)/2 = O(n^2)$

Recursive formulation

- * To sort $A[i \dots n-1]$
 - * Find minimum value in segment and move to $A[i]$
 - * Apply Selection Sort to $A[i+1 \dots n-1]$
- * Base case
 - * Do nothing if $i = n-1$

Selection Sort, recursive

```
SelectionSort(A,start,n) // Sort A from start to n-1
```

```
if (start >= n-1)  
    return;
```

```
// Locate minimum element and move to start of segment
```

```
minpos = start;  
for (i = start+1; i < n; i++)  
    if (A[i] < A[minpos])  
        minpos = i;
```

```
swap(A,start,minpos)
```

```
// Recursively sort the rest
```

```
SelectionSort(A,start+1,n)
```


Alternative calculation

- * $t(n)$, time to run selection sort on length n
 - * n steps to find minimum and move to position 0
 - * $t(n-1)$ time to run selection sort on $A[1]$ to $A[n-1]$
- * **Recurrence**
 - * $t(n) = n + t(n-1)$
 $t(1) = 1$
 - * $t(n) = n + t(n-1) = n + ((n-1) + t(n-2)) = \dots =$
 $n + (n-1) + (n-2) + \dots + 1 = n(n+1)/2 = O(n^2)$