

RDBMS and SQL

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Query processing

- Translate the query from SQL into relational algebra
- Evaluate the relational algebra expression
- Challenges
 - Many equivalent relational algebra expressions
 $\sigma_{salary < 75000}(\pi_{salary}(instructor))$ vs $\pi_{salary}(\sigma_{salary < 75000}(instructor))$
 - Many ways to evaluate a given expression
- Query plan
 - Annotate the expression with a detailed evaluation strategy key values
 - Use index on *salary* to find instructors with $salary < 75000$
 - Or, scan entire relation, discard rows with $salary \geq 75000$

Query optimization

- Choose plan with lowest cost
- Maintain **database catalogue** — number of tuples in each relationn, size of tuples, ...
- Assess cost in terms of disk access and transfer, CPU time, ...
- For simplicity, ignore in-memory costs (CPU time), restrict to disk access
- Disk accesses
 - Relation r occupies b_r blocks
 - **Disk seeks** — time t_S per seek
 - **Block transfers** — time t_T per transfer

Selection

- Linear search *1 seek, b_r transfers*

- Clustering index — index height h_i

- Equality on key
- Equality on nonkey

- Secondary index (key, non-key)

- Clustering index, comparison on A

- Sorted on A
- Not sorted on A

- Boolean combinations

- Conjunctive selection using one index
- Conjunctive selection using composite index
- Disjunction, negation, ...



External merge sort

- N records, b_r blocks, M blocks in memory
- Compute sorted runs of size M
- Merge sorted runs
- Complexity
 - b_r/M sorted runs, $\lceil \log_{M-1}(b_r/M) \rceil$ merge passes
 - Block transfers — $b_r (2\lceil \log_{M-1}(b_r/M) \rceil + 1)$
 - Block seeks — $2\lceil b_r/M \rceil + b_r (2(\lceil \log_{M-1}(b_r/M) \rceil - 1))$

Nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)

- Complexity

- $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation
- Block transfers: $b_r + n_r \cdot b_s$
- Block seeks: $b_r + n_r$ — inner relation read sequentially
- Special case: smaller relation fits in memory



Student $b_r = 100$
 $n_r = 5000$
Takes $b_s = 400$

$$n_r \cdot b_s = 2 \times 10^6$$
$$+ b_r = 2,000,100$$

Takes

Student

$b_r = 400$
 $n_r = 10000$
Student $b_s = 100$

$$n_r \cdot b_s = 1 \times 10^6$$
$$+ b_r = 1,000,400$$

Block nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)

- Complexity

- $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation

- Block transfers $\underbrace{b_r + b_r \cdot b_s}_{\text{vs } n_r \cdot b_s}$

- Block seeks: $\underbrace{b_r + b_r}_{2b_r}$

Student 100 + 100 × 400
Takes 200

Takes 400 + 100 × 400
Student 800
×

What is the output size ?

Indexed nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)
- Complexity
 - $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation
 - Total cost: $b_r(t_T + t_S) + n_r \cdot c$
 - c is cost of single selection on s

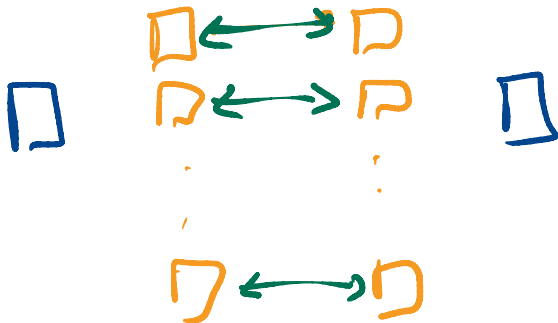
Merge join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)
- Complexity
 - $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation
 - Assume relations are sorted (add cost of sorting)
 - Block transfers: $b_r + b_s$
 - Block seeks: $\lceil b_r/b_b \rceil + \lceil b_s/b_b \rceil$
 - Read a chunk of blocks b_b at a time



Hash join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)
- Hash function on join attribute *A*, n_h output values
- Join each pair of hash buckets — build index and probe



- Choose plan with lowest cost

SQL $\rightarrow$ Relational Algebra



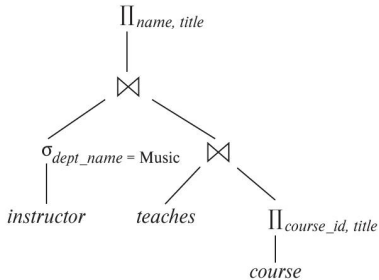
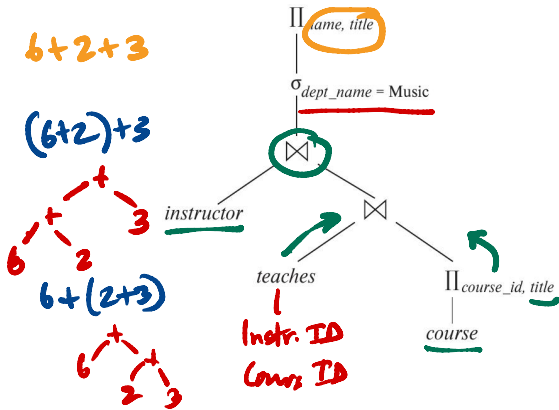
Choose best implementation
of each operation

Query optimization

- Choose plan with lowest cost
- *Find names and course titles of courses taught by instructors from Music Dept*

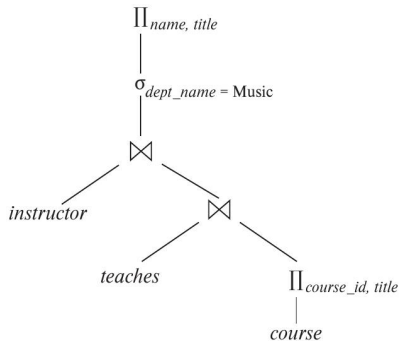
Query optimization

- Choose plan with lowest cost
- *Find names and course titles of courses taught by instructors from Music Dept*

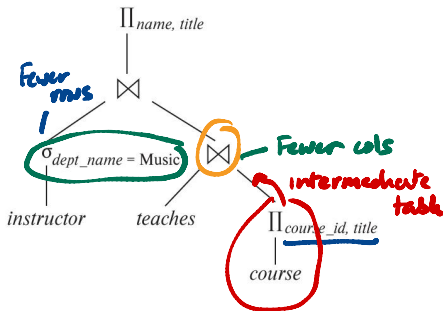


Query optimization

- Choose plan with lowest cost
- *Find names and course titles of courses taught by instructors from Music Dept*

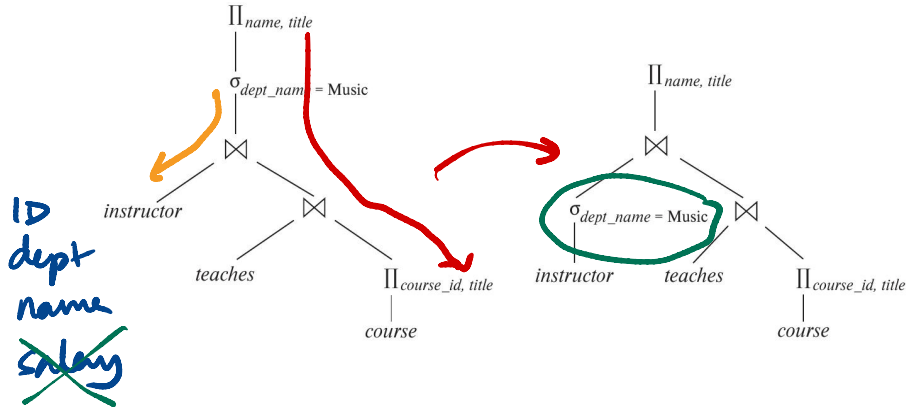


$$\Pi_n \left(\sigma_{dept_name = Music} (inst. \bowtie (teaches \bowtie course)) \right)$$



Query optimization

- Choose plan with lowest cost
- *Find names and course titles of courses taught by instructors from Music Dept*



Transforming expressions

σ_{θ_1}
↓
 σ_{θ_2}

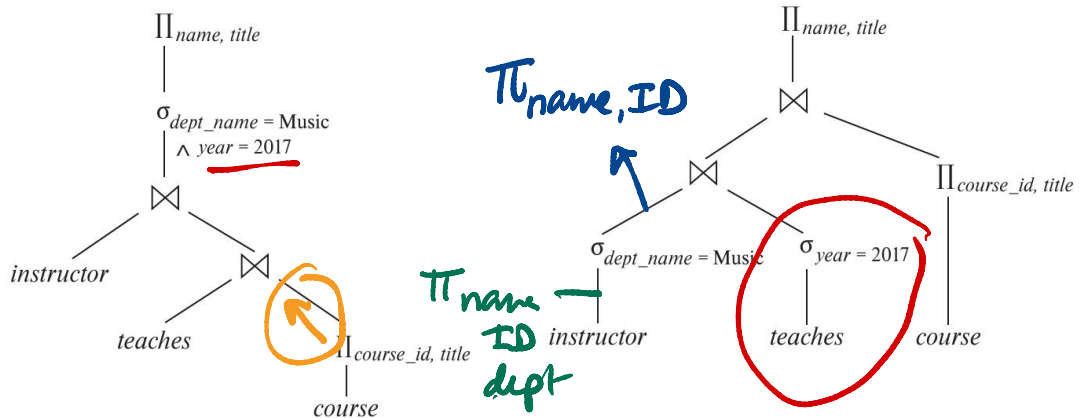


σ_{θ_2}
↓
 σ_{θ_1}



Systematic set of rules to transform
expressions, preserve & output

Transforming expressions



Maintaining a database catalogue

- n_r — number of tuples in r ✓
- b_r — number of blocks used by r ✓
- ℓ_r — size of a tuple in r ✓
- f_r — blocking factor of r , how many tuples fit in a block ✓
- $V(A, r)$ — number of distinct values of attribute A in r ✓
 - Store distribution of values as histogram

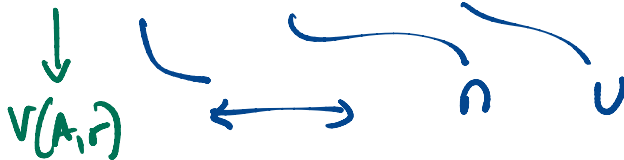
Background update

Pandas → data summary

Estimating output of an operation

- Selection

- Simple, range, conjunction, disjunction



Estimating output of an operation

- Selection
 - Simple, range, conjunction, disjunction
- Join
 - Keys and non-keys

Estimating output of an operation

- Selection
 - Simple, range, conjunction, disjunction
- Join
 - Keys and non-keys
- Projection

Estimating output of an operation

- Selection
 - Simple, range, conjunction, disjunction
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- Aggregation

Estimating output of an operation

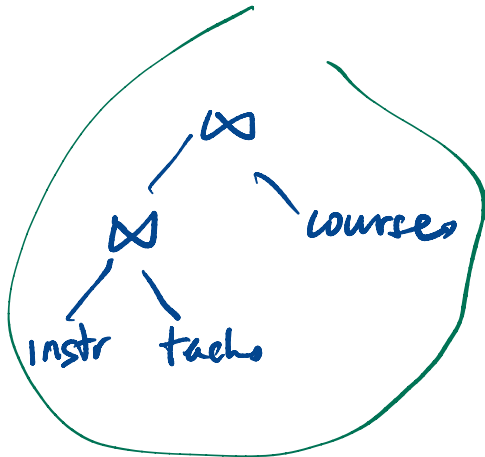
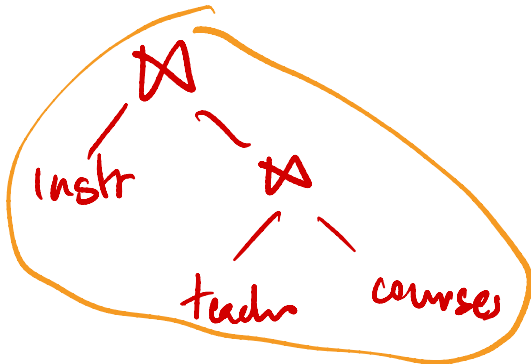
- Selection
 - Simple, range, conjunction, disjunction
- Join
 - Keys and non-keys
- Projection
- Aggregation
- Set operations

Estimating output of an operation

- Selection
 - Simple, range, conjunction, disjunction
- Join
 - Keys and non-keys
- Projection
- Aggregation
- Set operations
- Outer joins

Join ordering

$$(r_1 \bowtie (r_2 \bowtie r_3))$$



Join ordering

$M_1 \times M_2$
 r, c c, k

cost — $r \cdot c \cdot k$

output — $r \times k$

1×1
 $M_1 \times M_2 \times M_3$
 1×100 100×1 1×100
 100×100

Heuristics

- Perform selection early

✓ Dept = Music

✓ year = 2017

Heuristics

- Perform selection early
- Perform projection early

$\pi_{course\ id, title}$

- Perform selection early
- Perform projection early
- Perform most restrictive selection/join first

Query planning

Multiple low level operations $\Rightarrow$ One high level op

Buy ticket

1. Check avail.
2. Choose flight
3. Pay

What guarantees
should
transactions
provide

Desirable properties

- Atomicity

All or nothing

Entire effect holds, or no change

buy discounted item



Unavailable



Desirable properties

- Atomicity
- Consistency

dept_name in instructor

is a foreign key in dept

Bank transfer
into a bal

Insert a new dept, add instructor

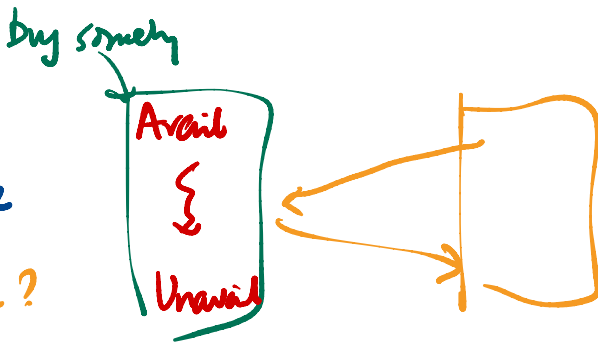
$A \xrightarrow{x} B$
 $A-x \quad B+x$

Desirable properties

- Atomicity
- Consistency
- Isolation

No
Interference
Performance?

Atomicity in the presence of concurrency



Desirable properties

- Atomicity
- Consistency
- Isolation
- Durability

Persistence of outcome

Desirable properties

- Atomicity
- Consistency
- Isolation
- Durability
- ACID properties

Transaction logs

- Log each update **before** it happens
- Rollback updates in case of failure

