

RDBMS and SQL

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Recap

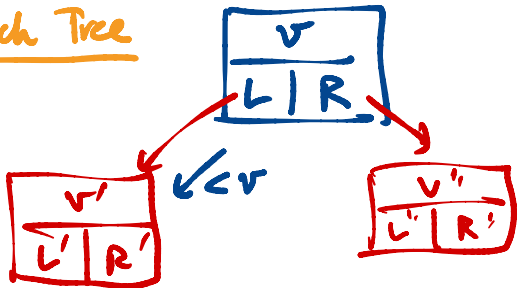
- Store tables on disk
- Transfer data in blocks - seek, transfer
- Maintain index

Search Tree

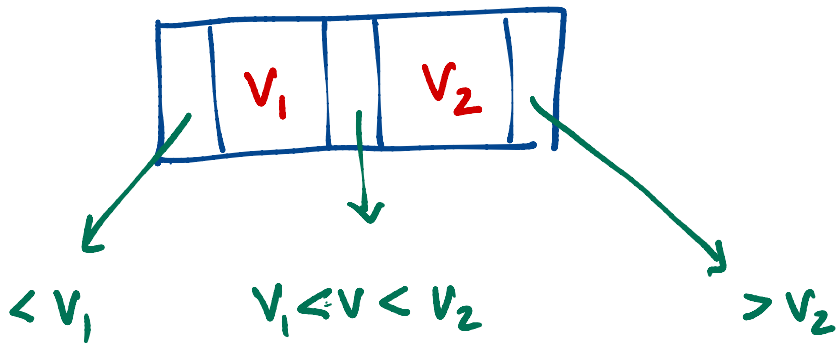
k levels $\rightarrow 2^0 + 2^1 + \dots + 2^{k-1}$

$$= 2^k - 1 - \text{size } N$$

$$k = \log N$$



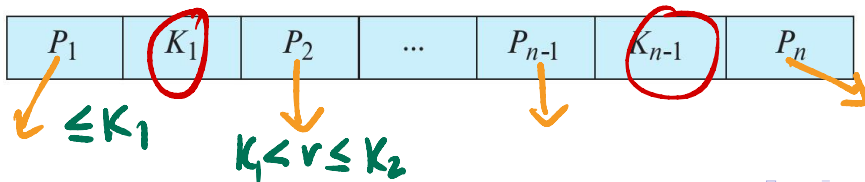
Generalize to 3-ary trees



Search trees

- Binary search trees
 - Binary search on dynamic data
 - Balanced tree has logarithmic height
- Block-based access
 - Binary tree node has one search key value, two pointers
 - Block can hold much more
- Generalize to multiple key values, multiple pointers

Attribute



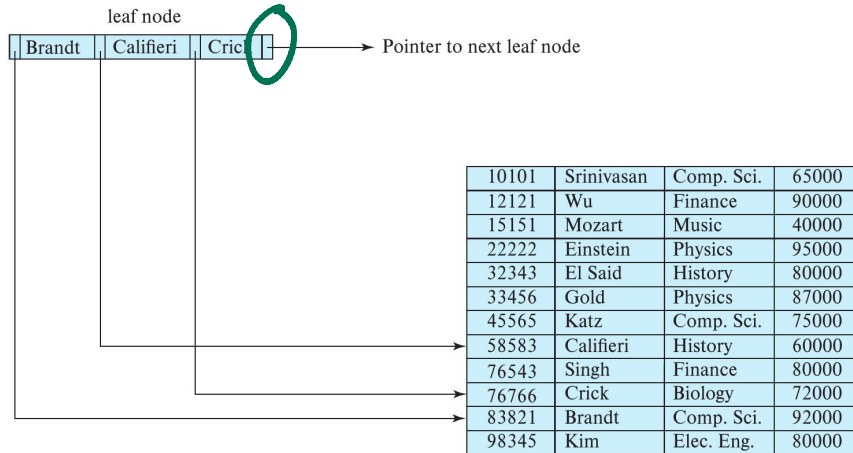
1 TB disk - 10^{12}

$\Rightarrow$ 4096 Byte blocks $\approx 10^9$ blocks

$$\downarrow$$
$$\log_2 10^9 \approx 30$$

B+ trees

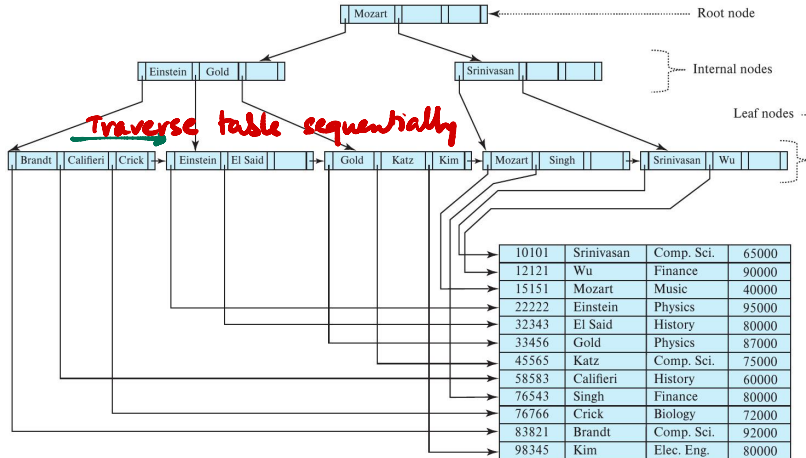
- Leaf nodes form a dense index — linked list of leaves, each one block



instructor file

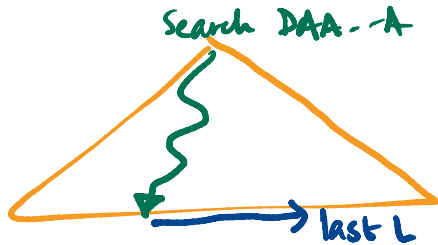
B+ trees

- Leaf nodes form a dense index — linked list of leaves
- Non-Leaf nodes form a sparse index



✓ Name = "Brandt"

✓ Name starts with (D) - L Range of values



B+ trees

- Leaf nodes form a dense index — linked list of leaves
- Non-leaf nodes form a sparse index
- Constraints — assume n keys and pointers can fit in a block
 - Each leaf has at least $\lceil (n-1)/2 \rceil$ key values
 - Each non-leaf has at least $\lceil n/2 \rceil$ pointers
 - Height of the tree is proportional to $\log_{n/2}(n)$

Query processing

- Translate the query from SQL into relational algebra
- Evaluate the relational algebra expression

Query processing

- Translate the query from SQL into relational algebra
- Evaluate the relational algebra expression
- Challenges
 - Many equivalent relational algebra expressions
 $\sigma_{salary < 75000}(\pi_{salary}(instructor))$ vs $\pi_{salary}(\sigma_{salary < 75000}(instructor))$
 - Many ways to evaluate a given expression

Query processing

- Translate the query from SQL into relational algebra
- Evaluate the relational algebra expression

- Challenges

- Many equivalent relational algebra expressions

$\sigma_{salary < 75000}(\pi_{salary}(instructor))$ vs $\pi_{salary}(\sigma_{salary < 75000}(instructor))$

- Many ways to evaluate a given expression

- Query plan

- Annotate the expression with a detailed evaluation strategy key values
 - Use index on *salary* to find instructors with *salary* < 75000
 - Or, scan entire relation, discard rows with *salary* ≥ 75000

Query optimization

- Choose plan with lowest cost
- Maintain **database catalogue** — number of tuples in each relationn, size of tuples, ...
- Assess cost in terms of disk access and transfer, CPU time, ...
- For simplicity, ignore in-memory costs (CPU time), restrict to disk access

Query optimization

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- Assess cost in terms of disk access and transfer, CPU time, ...
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- Disk accesses
 - Relation r occupies b_r blocks
 - **Disk seeks** — time t_S per seek
 - **Block transfers** — time t_T per transfer

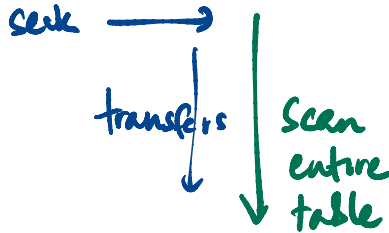
Query optimization

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- Disk accesses
 - Relation r occupies b_r blocks
 - **Disk seeks** — time t_S per seek
 - **Block transfers** — time t_T per transfer
- Other factors — buffer management etc

Selection

- Linear search

$$t_s + b_r \cdot t_r$$



$$\nabla_{\theta}(r)$$

Selection

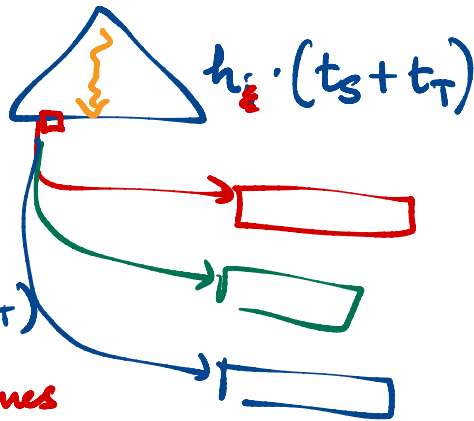
- Linear search
- Clustering index — index height h_i
 - Equality on key
 - Equality on nonkey

$$\underline{\underline{=}} \quad (h+1)(t_s+t_T)$$

$$h(t_s+t_T) + b(\cancel{t_s+t_T})$$

$\downarrow$
no. of values

$$+ 1 + b \cdot t_T$$



Selection

- Linear search
- Clustering index — index height h_i — table is ordered by this
 - Equality on key
 - Equality on nonkey
- Secondary index (key, non-key)

$$h(t_s + t_T) + b(t_s + t_T)$$

Same as before

Selection

- Linear search
- Clustering index — index height h_i
 - Equality on key
 - Equality on nonkey
- Secondary index (key, non-key)
- Clustering index, comparison on A
 - Sorted on A
 - Not sorted on A

$$v_1 \leq A \leq v_2 = \text{size } n \text{ blocks}$$
$$h(b_s + b_T) + b_s + n \cdot b_T$$

Selection

- Linear search
- Clustering index — index height h_i
 - Equality on key
 - Equality on nonkey
- Secondary index (key, non-key)
- Clustering index, comparison on A
 - Sorted on A
 - Not sorted on A
- Boolean combinations
 - Conjunctive selection using one index
 - Conjunctive selection using composite index
 - Disjunction, negation, ...

$$\sigma_{\theta_1 \wedge \theta_2}(\sigma)$$



— Smaller if two conditions

$$J_{\text{oin}} = \nabla_{\theta} (r_1 \times r_2)$$

Sorting

- In-memory sorting vs sorting on disk

Sorting

- In-memory sorting vs sorting on disk
- Merging sorted lists — varieties

Merging — Combine 2 sorted lists into 1

Duplicates — Eliminate — Union

— Keep only duplicates — Intersect

— Set difference

Sorting

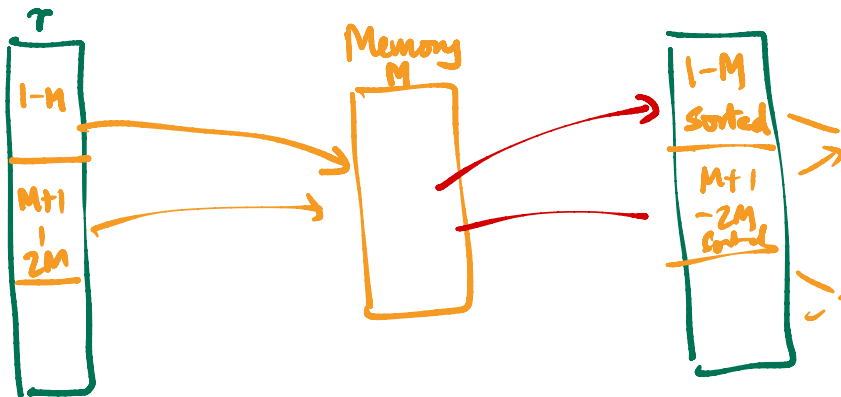
- In-memory sorting vs sorting on disk
- Merging sorted lists — varieties
- Traditional merge sort

External merge sort

- N records, b_r blocks, M blocks in memory

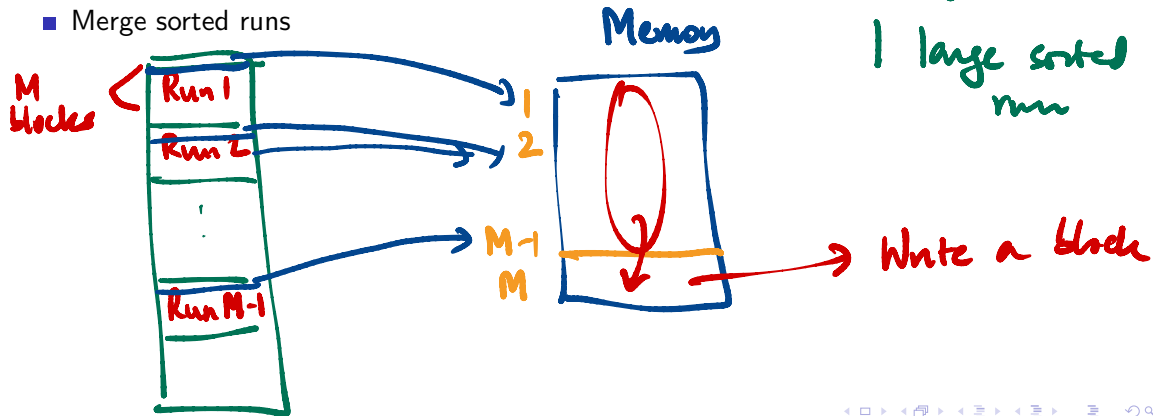
External merge sort

- N records, b_r blocks, M blocks in memory
- Compute sorted runs of size M



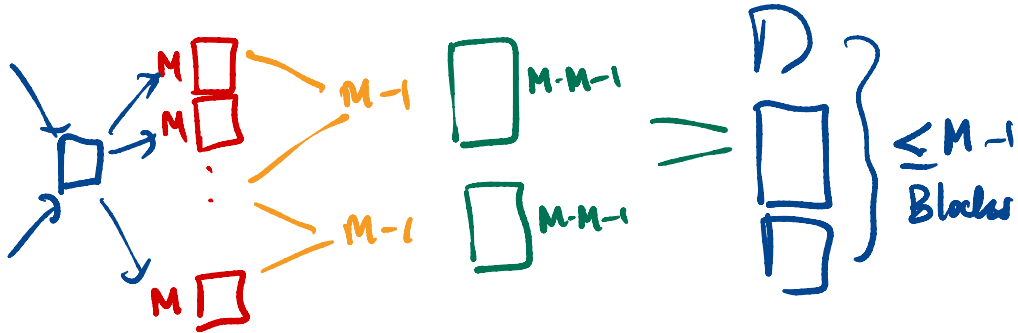
External merge sort

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- Merge sorted runs



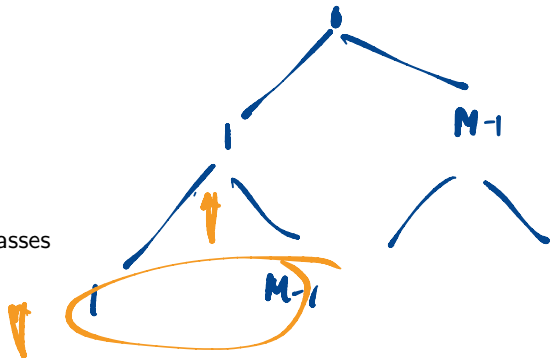
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External merge sort

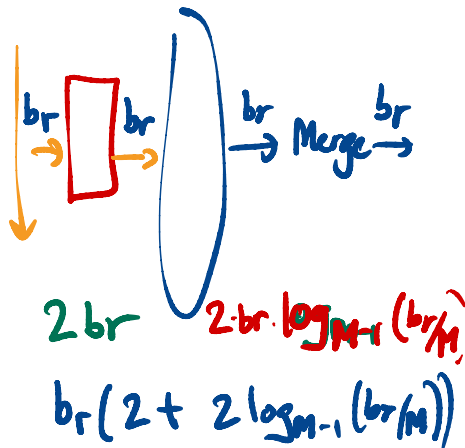
- N records, b_r blocks, M blocks in memory
- Compute sorted runs of size M
- Merge sorted runs
- Complexity
 - b_r/M sorted runs, $\lceil \log_{M-1}(b_r/M) \rceil$ merge passes



External merge sort

- N records, b_r blocks, M blocks in memory
- Compute sorted runs of size M
- Merge sorted runs
- Complexity
 - b_r/M sorted runs, $\lceil \log_{M-1}(b_r/M) \rceil$ merge passes
 - Block transfers — $b_r (2 \lceil \log_{M-1}(b_r/M) \rceil + 1)$
 - Why not $b_r (2 \lceil \log_{M-1}(b_r/M) \rceil + 2)$?

Last round of writing is ignored — "pipeline"



External merge sort

- N records, b_r blocks, M blocks in memory
- Compute sorted runs of size M
- Merge sorted runs
- Complexity
 - b_r/M sorted runs, $\lceil \log_{M-1}(b_r/M) \rceil$ merge passes
 - Block transfers — $b_r (2\lceil \log_{M-1}(b_r/M) \rceil + 1)$
 - Why not $b_r (2\lceil \log_{M-1}(b_r/M) \rceil + 2)$?
 - Block seeks — $2\lceil b_r/M \rceil + b_r (2(\lceil \log_{M-1}(b_r/M) \rceil - 1))$

Computing joins

- Running example

- *Student* ⋈ *Takes*

Computing joins

■ Running example

■ *Student* ⋈ *Takes*

■ *Student* — 5000 rows, 100 blocks

■ *Takes* — 10000 rows, 400 blocks

— 50 rows / block
— 25 rows / block

Nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)

Nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)
- Complexity
 - $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation

for each row in r
for each row in s

Nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)
- Complexity
 - $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation
 - Block transfers: $b_r + n_r \cdot b_s$

outer L for each row in r , scan s

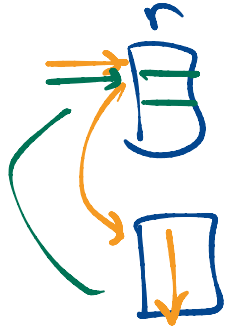
Nested-loop join

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- Complexity

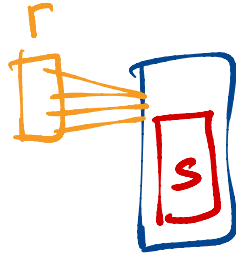
- $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation
- Block transfers: $b_r + n_r \cdot b_s$
- Block seeks: $b_r + n_r$ — inner relation read sequentially

=
seeks of s



Nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)
- Complexity
 - $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation
 - Block transfers: $b_r + \cancel{r} \cdot b_s$
 - Block seeks: $b_r + n_r$ — inner relation read sequentially
 - Special case: smaller relation fits in memory



Block nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)

Block nested-loop join

- (5000 rows, 100 blocks) *Student* $\bowtie$ *Takes* (10000 rows, 400 blocks)
- Complexity
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Block nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)

- Complexity

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- Block transfers: $b_r + b_r \cdot b_s$

$$n_r \cdot b_s$$

Block nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)

- Complexity

- $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation

- Block transfers: $b_r + b_r \cdot b_s$

- Block seeks: $b_r + b_r = 2b_r$

b_r

Indexed nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)

Indexed nested-loop join

- (5000 rows, 100 blocks) *Student* $\bowtie$ *Takes* (10000 rows, 400 blocks)
- Complexity
 - $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation

for each row in r
search for A in s

Indexed nested-loop join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)
- Complexity
 - $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation
 - Total cost: $b_r(t_T + t_S) + n_r \cdot c$
 - c is cost of single selection on s

Merge join

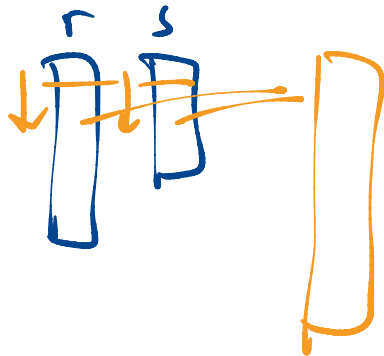
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Merge join

- (5000 rows, 100 blocks) *Student* $\bowtie$ *Takes* (10000 rows, 400 blocks)
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 - Assume relations are sorted (add cost of sorting)

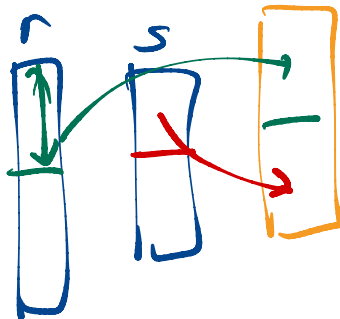
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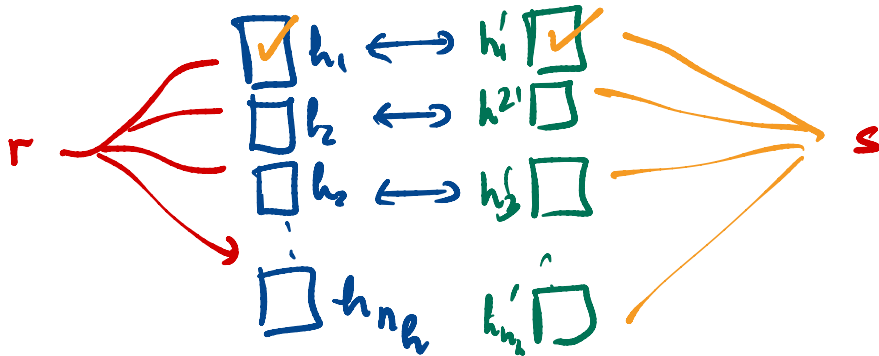
Merge join

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- Complexity
 - $r \bowtie_{\theta} s$ — r is outer relation, s is inner relation
 - Assume relations are sorted (add cost of sorting)
 - Block transfers: $b_r + b_s$
 - Block seeks: $\lceil b_r/b_b \rceil + \lceil b_s/b_b \rceil$
 - Read a chunk of blocks b_b at a time



Hash join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)
- Hash function on join attribute A , n_h output values



Hash join

- (5000 rows, 100 blocks) *Student* ⋈ *Takes* (10000 rows, 400 blocks)
- Hash function on join attribute *A*, n_h output values
- Join each pair of hash buckets — build index and probe

