

RDBMS and SQL

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Lecture 4, 4 September 2025

Relational algebra

- Select *Rows*
 - Project *Columns*
 - Join — cartesian product + select
 - Natural join — *implicit equality on same col names*
 - Set operations
 - Union, intersection, set difference
 - Assignment, renaming *Self join*
- Table.Column*

Relational algebra — Examples

`Instructor(ID,name,dept_name,salary)`

- Find all faculty members from Physics who earn more than **at least one** faculty member from Comp.Sci.

Witness

for each Physics faculty

for each CS faculty

Check salary & report

<i>ID</i>	<i>name</i>	<i>dept_name</i>	<i>salary</i>
10101	Srinivasan	Comp. Sci.	65000
12121	Wu	Finance	90000
15151	Mozart	Music	40000
22222	Einstein	Physics	95000
32343	El Said	History	60000
33456	Gold	Physics	87000
45565	Katz	Comp. Sci.	75000
58583	Califieri	History	62000
76543	Singh	Finance	80000
76766	Crick	Biology	72000
83821	Brandt	Comp. Sci.	92000
98345	Kim	Elec. Eng.	80000

Instructor

Relational algebra — Examples

`Instructor(ID,name,dept_name,salary)`

- Find all faculty members from Physics who earn more than **at least one** faculty member from Comp.Sci.

for each Instructor

if dept = Physics

for each Instructor

if dept = CS

z

<i>ID</i>	<i>name</i>	<i>dept_name</i>	<i>salary</i>
10101	Srinivasan	Comp. Sci.	65000
12121	Wu	Finance	90000
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Instructor

Relational algebra — Examples

`Instructor(ID,name,dept_name,salary)`

- Find all faculty members from Physics who earn more than **at least one** faculty member from Comp.Sci.

Self join

$\pi_{\text{all 4 cols}} [\rho_L(\text{Instructor}) \bowtie_{\theta} \rho_R(\text{Instructor})]$

all 4
cols
from left

$\theta: L.\text{dept_name} = \text{Physics} \wedge$
 $R.\text{dept_name} = \text{Comp Sci} \wedge$
 $L.\text{salary} > R.\text{salary}$

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Instructor

Relational algebra — Examples

`Instructor(ID, name, dept_name, salary)`

- Find all faculty members from Physics who earn more than **at least one** faculty member from Comp.Sci.

Smarter iteration

First pass →

compute min sal
in CS

Second pass →

check all Physics
salaries against
min CS

Claim: Can't do in reln algebra

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10101	Srinivasan	Comp. Sci.	65000
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76766	Crick	Biology	72000
83821	Brandt	Comp. Sci.	92000
98345	Kim	Elec. Eng.	80000

Instructor

Relational algebra — Examples

`Instructor(ID,name,dept_name,salary)`

- Find all faculty members from Physics who earn more than **every** faculty member from Comp.Sci.

Smart Iteration

1. Compute Max CS
2. Check Physics > MaxCS

Relational Algebra?

ID	name	dept_name	salary
10101	Srinivasan	Comp. Sci.	65000
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98345	Kim	Elec. Eng.	80000

Instructor

Relational algebra — Examples

`Instructor(ID,name,dept_name,salary)`

- Find all faculty members from Physics who earn more than **every** faculty member from Comp.Sci.

Witness for exclusion from output

In Physics, cannot less than
someone in CS

Same as earlier self join but
 $L.salary < R.salary$

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98345	Kim	Elec. Eng.	80000

Instructor

Relational algebra — Examples

`Instructor(ID, name, dept_name, salary)`

- Find all faculty members from Physics who earn more than **every** faculty member from Comp.Sci.

$R_1 \leftarrow \pi_{\text{left}}(\sigma_2(\text{Inst.}) \bowtie \theta_{\text{Exclusion}} \rho_R(\text{Inst.}))$

$R_2 \leftarrow \pi_{\text{dept_name} = \text{Physics}}(\text{Inst.})$

$R_2 \setminus R_1$

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Instructor

Relational algebra — Examples

`Instructor(ID,name,dept_name,salary)`

- Find the faculty member(s) with the minimum salary.

Not min $\Rightarrow$ there is witness

$\text{NotMin} = \pi_{\text{left}} (S_L(I) \bowtie S_R(I))$
 $\downarrow$
 $L.\text{sal} > R.\text{sal}$

$\text{Instructor} \sim \text{NotMin}$

<i>ID</i>	<i>name</i>	<i>dept_name</i>	<i>salary</i>
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Instructor

Relational algebra — Examples

`Instructor(ID,name,dept_name,salary)`

- Find the faculty member(s) with the minimum salary.

Min column (Relation)

Min salary (Instructor) Create new operators

Max ? L.sal < R.sal Not Max
Max col (R)

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98345	Kim	Elec. Eng.	80000

Instructor

Relational algebra — Examples

Instructor(ID,name,dept_name,salary)

- Find the faculty member(s) with the minimum salary.

Smart Iteration

1. Find Min CS
2. Check Phy > Min CS

Hidden x

Instructor $\bowtie$ $\pi_{\text{salary}}(\text{Min CS, (Instructor)})$

$\downarrow$
L.dept_name = Physics $\wedge$
L.salary > R.salary

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Instructor

min ES
set

Relational algebra — Examples

Instructor(ID,name,dept_name,salary)

"Grouping"

- Find the faculty member(s) with the maximum salary, department-wise.

1 row $\leftarrow \text{Max}_{\text{CS}, \text{salary}}(\text{Instructor})$

1 row $\leftarrow \text{Max}_{\text{Physic}, \text{salary}}(\text{Instructor})$

$\text{Max}_{\text{EE}, \text{salary}}(\text{Instructor})$

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Instructor

Relational algebra — Examples

✓ family(ID, name, gender)

~~relation(ID1, ID2, relationship)~~

- Compute the relation

sister(ID1, ID2) — ID1 is a sister of ID2

only parent

Given

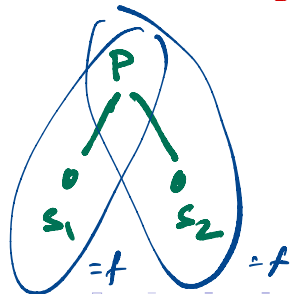
✓ parent(ID₁, ID₂)

⇓

mother(ID₁, ID₂)?

Family ID ID=ID₁ parents
^
gender=f

$(P, s_1) \times (P, s_2) \times (s_1, f) \times (s_2, f)$



Relational algebra — Examples

family(ID,name,gender)

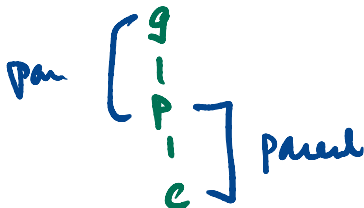
~~relation(ID1,ID2,relationship)~~

parent(ID₁, ID₂)

- Compute grandparent(ID₁, ID₂) —
ID₁ is grandparent of ID₂

(P₁, P₂), (P₂, P₃)

(P₁, P₃)



Relational algebra — Examples

family(ID,name,gender)

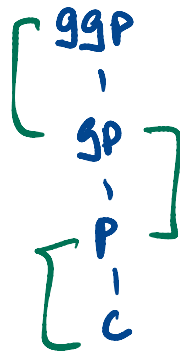
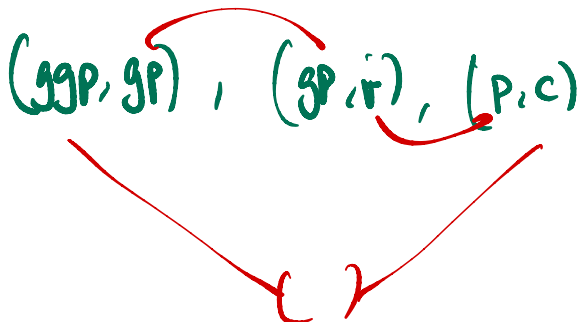
~~relation(ID1,ID2,relationship)~~

parent(ID₁,ID₂)

- Compute

greatgrandparent(ID1,ID2) — ID1

is greatgrandparent of ID2



Relational algebra — Examples

family(ID,name,gender)

~~relation(ID1,ID2,relationship)~~

parent(ID₁,ID₂)

- Can you compute ancestor(ID₁,ID₂) in general?

✓
parent $\cup$ grandparent $\cup$ greatgrandparent

ancestor upto 3 gens

k^{th} gen ancestor $\Rightarrow k-1$

a
|
P₁
|
P₂
|
⋮
|
P_k
|
c

Relational algebra — Examples

family(ID,name,gender)

~~relation(ID1,ID2,relationship)~~

parent (ID₁, ID₂)

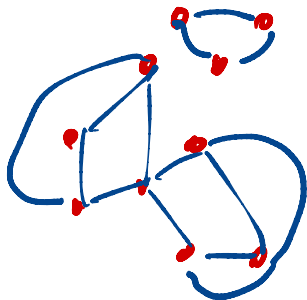
- Can you compute ancestor(ID₁,ID₂)
in general?

↳ Transitive Closure of Parent

Cannot be done

First Order (Predicate) logic

$\forall x \exists y x < y$
 $\forall x \in \mathbb{R} \exists y \in \mathbb{R} x < y$



Relational algebra — Examples

family(ID,name,gender)

relation(ID1,ID2,relationship)

- Can you compute `ancestor(ID1,ID2)` in general?

$\forall$
 $\wedge$
 $\neg$

$\exists x$
 $\forall x$

$R(x,y)$ $P(x,y,z)$

Transitive closure is not expressible in
First Order logic (FOL)

Relational Algebra is complete w.r.t. FOL queries