

PDSP2025, Lecture 22, 4 November 2025

Searching and Sorting

Setup

- Use `time` library to time executions

```
In [1]: import time
```

Naive search by scanning the list

```
In [2]: def naivesearch(v,l):  
        for x in l:  
            if v == x:  
                return(True)  
        return(False)
```

Binary search

```
In [3]: def binarysearch(v,l):  
        if l == []:  
            return(False)  
  
        m = len(l)//2  
  
        if v == l[m]:  
            return(True)  
  
        if v < l[m]:  
            return(binarysearch(v,l[:m]))  
        else:  
            return(binarysearch(v,l[m+1:]))
```

Checking correctness on input `[0,2,...,50]`

```
In [4]: l = list(range(0,51,2))  
  
        for i in range(51):  
            print((i,naivesearch(i,l)),end=",")  
        print()  
  
        for i in range(51):  
            print((i,binarysearch(i,l)),end=",")  
        print()
```

```
(0, True),(1, False),(2, True),(3, False),(4, True),(5, False),(6, True),
(7, False),(8, True),(9, False),(10, True),(11, False),(12, True),(13, False),
(14, True),(15, False),(16, True),(17, False),(18, True),(19, False),
(20, True),(21, False),(22, True),(23, False),(24, True),(25, False),(26,
True),(27, False),(28, True),(29, False),(30, True),(31, False),(32, True),
(33, False),(34, True),(35, False),(36, True),(37, False),(38, True),(39,
False),(40, True),(41, False),(42, True),(43, False),(44, True),(45, False),
(46, True),(47, False),(48, True),(49, False),(50, True),
(0, True),(1, False),(2, True),(3, False),(4, True),(5, False),(6, True),
(7, False),(8, True),(9, False),(10, True),(11, False),(12, True),(13, False),
(14, True),(15, False),(16, True),(17, False),(18, True),(19, False),
(20, True),(21, False),(22, True),(23, False),(24, True),(25, False),(26,
True),(27, False),(28, True),(29, False),(30, True),(31, False),(32, True),
(33, False),(34, True),(35, False),(36, True),(37, False),(38, True),(39,
False),(40, True),(41, False),(42, True),(43, False),(44, True),(45, False),
(46, True),(47, False),(48, True),(49, False),(50, True),
```

Performance comparison across 10^4 worst case searches in a list of size 10^5

- Looking for odd numbers in a list of even numbers

```
In [5]: l = list(range(0,200000,2))

starttime = time.perf_counter()
for i in range(3001,23000,2):
    v = naivesearch(i,l)
elapsed = time.perf_counter() - starttime
print()
print("Naive search", elapsed)

starttime = time.perf_counter()
for i in range(3001,23000,2):
    v = binarysearch(i,l)
elapsed = time.perf_counter() - starttime
print()
print("Binary search", elapsed)
```

Naive search 17.956641599004797

Binary search 1.9248965570004657

Selection sort

```
In [6]: def SelectionSort(L):
    n = len(L)
    if n < 1:
        return(L)
    for i in range(n):
        # Assume L[:i] is sorted
        mpos = i
        # mpos is position of minimum in L[i:]
        for j in range(i+1,n):
            if L[j] < L[mpos]:
                mpos = j
        # L[mpos] is the smallest value in L[i:]
        (L[i],L[mpos]) = (L[mpos],L[i])
```

```
    # Now L[:i+1] is sorted
    return(L)
```

Selection sort performance is more or less the same for all inputs

```
In [7]: import random
        random.seed(2025)
        inputlists = {}
        inputlists["random"] = [random.randrange(100000) for i in range(5000)]
        inputlists["ascending"] = [i for i in range(5000)]
        inputlists["descending"] = [i for i in range(4999, -1, -1)]
        for k in inputlists.keys():
            tmplist = inputlists[k][:]
            starttime = time.perf_counter()
            SelectionSort(tmplist)
            elapsed = time.perf_counter() - starttime
            print(k, elapsed)
```

```
random 0.41388963800272904
ascending 0.3815801900054794
descending 0.390925444997265
```

Insertion sort, iterative

```
In [8]: def InsertionSort(L):
        n = len(L)
        if n < 1:
            return(L)
        for i in range(n):
            # Assume L[:i] is sorted
            # Move L[i] to correct position in L[:i]
            j = i
            while(j > 0 and L[j] < L[j-1]):
                (L[j], L[j-1]) = (L[j-1], L[j])
                j = j-1
            # Now L[:i+1] is sorted
        return(L)
```

Insertion sort preformance

- On already sorted input, performance is very good
- On reverse sorted input, performance is worse than selection sort

```
In [9]: import random
        random.seed(2025)
        inputlists = {}
        inputlists["random"] = [random.randrange(100000) for i in range(5000)]
        inputlists["ascending"] = [i for i in range(5000)]
        inputlists["descending"] = [i for i in range(4999, -1, -1)]
        for k in inputlists.keys():
            tmplist = inputlists[k][:]
            starttime = time.perf_counter()
            InsertionSort(tmplist)
            elapsed = time.perf_counter() - starttime
            print(k, elapsed)
```

```
random 0.5835713570049847
ascending 0.0002267620002385229
descending 1.1273996609961614
```

Insertion sort, recursive

Setup

- Set recursion limit to maxint, $2^{31} - 1$
 - This is the highest value Python allows

```
In [10]: import sys
sys.setrecursionlimit(2**31-1)
```

```
In [11]: def Insert(L,v):
    n = len(L)
    if n == 0:
        return([v])
    if v >= L[-1]:
        return(L+[v])
    else:
        return(Insert(L[:-1],v)+L[-1:])

def ISort(L):
    n = len(L)
    if n < 1:
        return(L)
    L = Insert(ISort(L[:-1]),L[-1])
    return(L)
```

Recursive insertion sort is slower than iterative

- Input of 2000 (40%) takes more time than 5000 for iterative
 - Overhead of recursive calls
- Performance pattern between unsorted, sorted and random is similar

```
In [12]: import random
random.seed(2025)

inputlists = {}
inputlists["random"] = [random.randrange(100000) for i in range(2000)]
inputlists["ascending"] = [i for i in range(2000)]
inputlists["descending"] = [i for i in range(1999,-1,-1)]
for k in inputlists.keys():
    tmplist = inputlists[k][:]
    starttime = time.perf_counter()
    ISort(tmplist)
    elapsed = time.perf_counter() - starttime
    print(k,elapsed)
```

```
random 2.9386179680004716
ascending 0.006556373999046627
descending 4.456001231003029
```

Merge sort

```
In [13]: def merge(A,B):
          (m,n) = (len(A),len(B))
          (C,i,j,k) = ([],0,0,0)
          while k < m+n:
              if i == m:
                  C.extend(B[j:])
                  k = k + (n-j)
              elif j == n:
                  C.extend(A[i:])
                  k = k + (n-i)
              elif A[i] < B[j]:
                  C.append(A[i])
                  (i,k) = (i+1,k+1)
              else:
                  C.append(B[j])
                  (j,k) = (j+1,k+1)
          return(C)
```

```
In [14]: def mergesort(A):
          n = len(A)

          if n <= 1:
              return(A)

          L = mergesort(A[:n//2])
          R = mergesort(A[n//2:])

          B = merge(L,R)

          return(B)
```

A simple input to check correctness

```
In [15]: mergesort([i for i in range(0,100,2)]+[j for j in range (1,100,2)])
```

```
Out[15]: [0,  
1,  
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99]

Performance on large inputs, 10^6 , random and sorted

```
In [16]: import random
random.seed(2025)
inputlists = {}
inputlists["random"] = [random.randrange(100000000) for i in range(100000)]
inputlists["ascending"] = [i for i in range(1000000)]
inputlists["descending"] = [i for i in range(999999, -1, -1)]
for k in inputlists.keys():
    tmplist = inputlists[k][:]
    starttime = time.perf_counter()
    mergesort(tmplist)
    elapsed = time.perf_counter() - starttime
    print(k, elapsed)
```

```
random 2.7101028859979124
ascending 1.4198947430049884
descending 1.4313436170050409
```

Quicksort

```
In [17]: def quicksort(L,l,r): # Sort L[l:r]
         if (r - l <= 1):
             return
         (pivot,lower,upper) = (L[l],l+1,l+1)
         for i in range(l+1,r):
             if L[i] > pivot: # Extend upper segment
                 upper = upper+1
             else: # Exchange L[i] with start of upper segment
                 (L[i], L[lower]) = (L[lower], L[i])
                 # Shift both segments
                 (lower,upper) = (lower+1,upper+1)
         # Move pivot between lower and upper
         (L[l],L[lower-1]) = (L[lower-1],L[l])
         lower = lower-1
         # Recursive calls
         quicksort(L,l,lower)
         quicksort(L,lower+1,upper)
         return
```

Small input to check correctness

```
In [18]: qlist = [1,3,5,0,2,4,17,2,-5,6,4,3]
         quicksort(qlist,4,8)
         print(qlist)
```

[1, 3, 5, 0, 2, 2, 4, 17, -5, 6, 4, 3]

Quicksort performance

- Random input of size 10^6
- Sorted inputs of size 2×10^4

```
In [19]: import random
         random.seed(2025)
         inputlists = {}
         inputlists["random"] = [random.randrange(100000000) for i in range(100000)]
         inputlists["ascending"] = [i for i in range(15000)]
         inputlists["descending"] = [i for i in range(14999,-1,-1)]
         for k in inputlists.keys():
             tmplist = inputlists[k][:]
             starttime = time.perf_counter()
             quicksort(tmplist,0,len(tmplist))
             elapsed = time.perf_counter() - starttime
             print(k,elapsed)
```

random 1.9635030670033302
ascending 4.193553910001356
descending 5.847825593002199

Randomized quicksort

- Choose the pivot position uniformly at random between `l` and `r-1`
- Swap pivot to `L[l]` and proceed as usual

```
In [20]: import random
def quicksortrand(L,l,r): # Sort L[l:r]
    if (r - l <= 1):
        return(L)

    # Choose a random postion between l and r-l as pivot, swap with L[l]
    randpivot = random.randrange(r-l)
    (L[l],L[l+randpivot]) = (L[l+randpivot],L[l])

    # Rest is same as before
    (pivot,lower,upper) = (L[l],l+1,l+1)
    for i in range(l+1,r):
        if L[i] > pivot: # Extend upper segment
            upper = upper+1
        else: # Exchange L[i] with start of upper segment
            (L[i], L[lower]) = (L[lower], L[i])
            # Shift both segments
            (lower,upper) = (lower+1,upper+1)
    # Move pivot between lower and upper
    (L[l],L[lower-1]) = (L[lower-1],L[l])
    lower = lower-1
    # Recursive calls
    quicksortrand(L,l,lower)
    quicksortrand(L,lower+1,upper)
    return(L)
```

```
In [21]: import random
random.seed(2025)
inputlists = {}
inputlists["random"] = [random.randrange(100000000) for i in range(100000)]
inputlists["ascending"] = [i for i in range(15000)]
inputlists["descending"] = [i for i in range (14999,-1,-1)]
inputlists["ascendingbig"] = [i for i in range(1000000)]
inputlists["descendingbig"] = [i for i in range (999999,-1,-1)]
for k in inputlists.keys():
    tmplist = inputlists[k][:]
    starttime = time.perf_counter()
    quicksortrand(tmplist,0,len(tmplist))
    elapsed = time.perf_counter() - starttime
    print(k,elapsed)
```

```
random 2.1547414349988685
ascending 0.01822181899478892
descending 0.018493495001166593
ascendingbig 1.622358353000891
descendingbig 1.747888535996026
```