

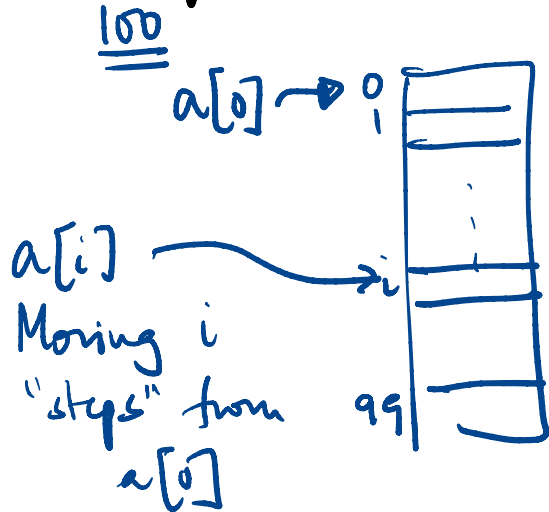
## Arrays

# Sequences

## Key-Value store

- Uniform type

Predefine its size a



Accessing  $a[i]$  takes same amount  
of time for any  $i$

"Random Access"

Swap  $a[i] \leftrightarrow a[j]$

$x, y = y, x$

$a[i], a[j] = a[j], a[i]$  — should not depend  
on  $i, j$

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List Sequence of "cells" that are linked together,  
like a train



Each cell could be far away from its neighbours

Accessing  $l[i]$  is proportional to  $i$

$$l[i], l[j] = l[j], l[i] \quad \text{— cost depends on } i \text{ \& } j$$

Why use a list?

Flexibility


Adding & deleting elements easily

Array  $a[0..99]$

Currently, using  $a[0..49]$

Insert a new value after  $a[30]$

$a[0] \dots a[29] \quad a[30] \quad a[31] \dots a[49]$



Need to make space

Shift  $a[49] \rightarrow a[50]$   
 $a[48] \rightarrow a[49]$

$a[31] \rightarrow a[32]$

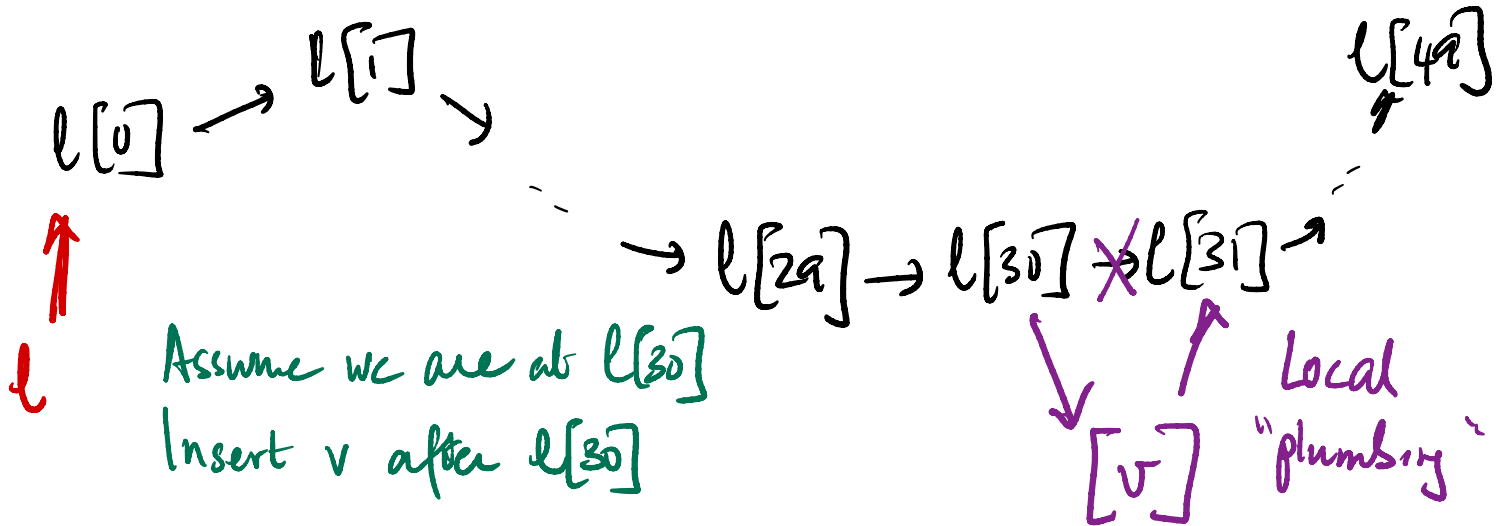
$a[31] = v$

Shifting values  
depending on  $i$

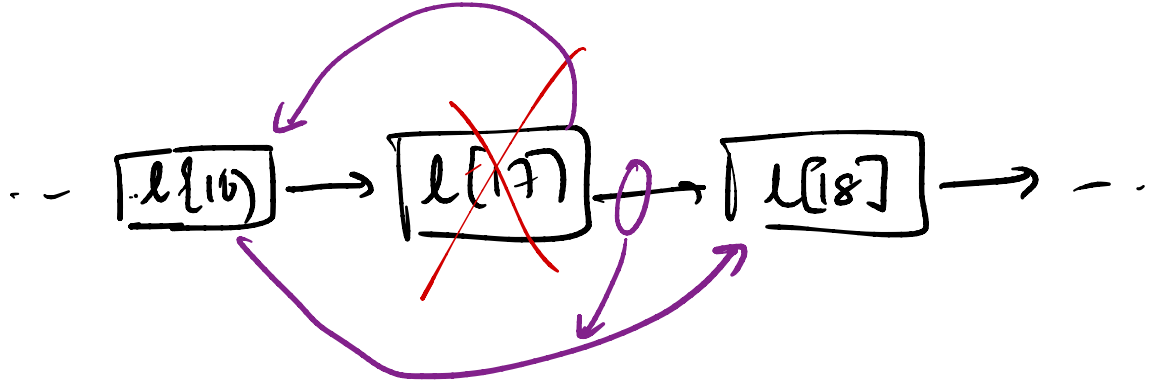
Delete  $a[17]$

$a[0] \dots a[16] \cancel{a[17]} a[18] \dots a[49]$

Need to shift to ensure contiguous storage, no gaps



Analogous for delete



Are Python lists arrays or lists?

Dictionaries?

$k_1 \rightarrow v_1$

$k_2 \rightarrow v_2$

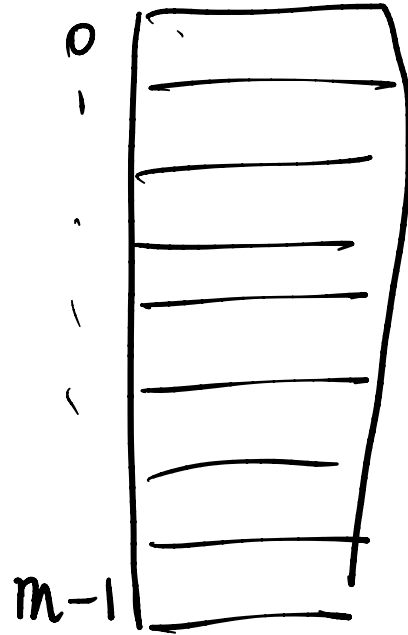
$\vdots$

$k_n \rightarrow v_n$

$v_1 \dots v_n$  are  
stored in locations  
 $0 \dots m-1$ ,  
but not in a  
fixed order

Function:  $k_i \rightarrow [0 \dots m-1]$

Storage is a  
fixed block,  
like array



Example key  $k \rightarrow$  write in binary  $\rightarrow$  number  $n_k$

$$n_k \bmod m \rightarrow [0 \dots m-1]$$

Space of keys is large, the range of locations is small

There will always be collisions  $f(k_1) = f(k_2)$

Strategies to deal with this

- Have a second function
- Move to next free location



These functions are called hash functions

$h$ : large set  $\rightarrow$  Very small set

Download a software package  $\rightarrow$  get a  
"fingerprint" or a "hash certificate"

SHA-256 — output is 256 bytes  
 $= 256 \times 8$  bits

Dropbox

# Python list?

Expanding array

`l = []`  $\rightsquigarrow$

Run out of space

Double the size

`l.append(x)` - fast  
`l.insert(0, x)` - slow

