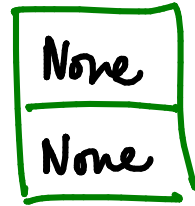
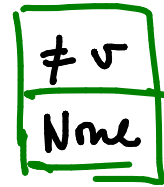


delete(*v*)

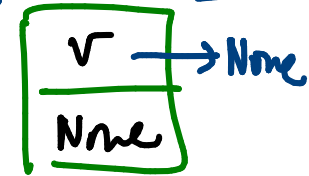
Case 1:
Do nothing



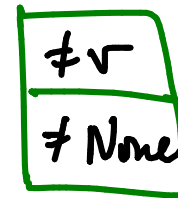
Case 2:
Do Nothing



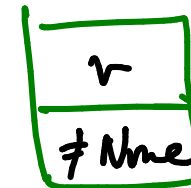
Case 3 $[v] \mapsto []$



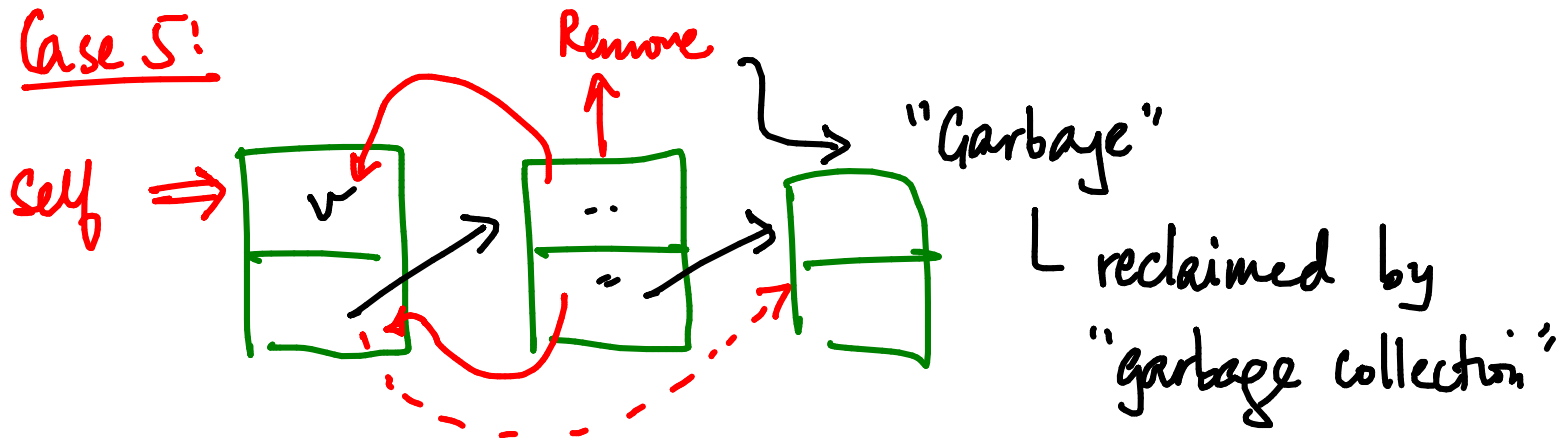
Case 4:
Recursive



Case 5



Case 5:



```

def delete(self, v):
    if self.isempty(): # Case 1
        return

    if self.next == None:
        if self.value == v:
            self.value = None # Case 3
            return # Cases 2 & 3
        if self.value == v: # Case 4
            self.value = self.next.value
            self.next = self.next.next
            return
        self.next.delete(v) # Case 5

```

next is not None →

Exercise: Replace this by a loop

Insert, append, delete

```
l[i] def value at pos (self, i):
```

$$e[i:j]$$
$$\ddot{f}_{ind}(v)$$

```
-- init --
```

Constructor

Other special functions

--str--

Invoked implicitly by `str(--)`
Should return string

Exercise: Print a list as $[v_1, v_2, \dots, v_n]$

Other special functions

--add--, --mult-- +, *

Object o with `--add--(v)` defined

$o + v \Rightarrow o.--add--(v)$

`self.value + v` ✗

`o1 + o2`

`o1.--add--(o2)`

`o1.value + o2`

`o1.value.--add--(o2)`

`v + self.value` ✓

`o1 + o2`

`o1.--add--(o2)`

`o2 + o1.value`

`o2.--add--(o1.value)`

`o2.value + o2.value`

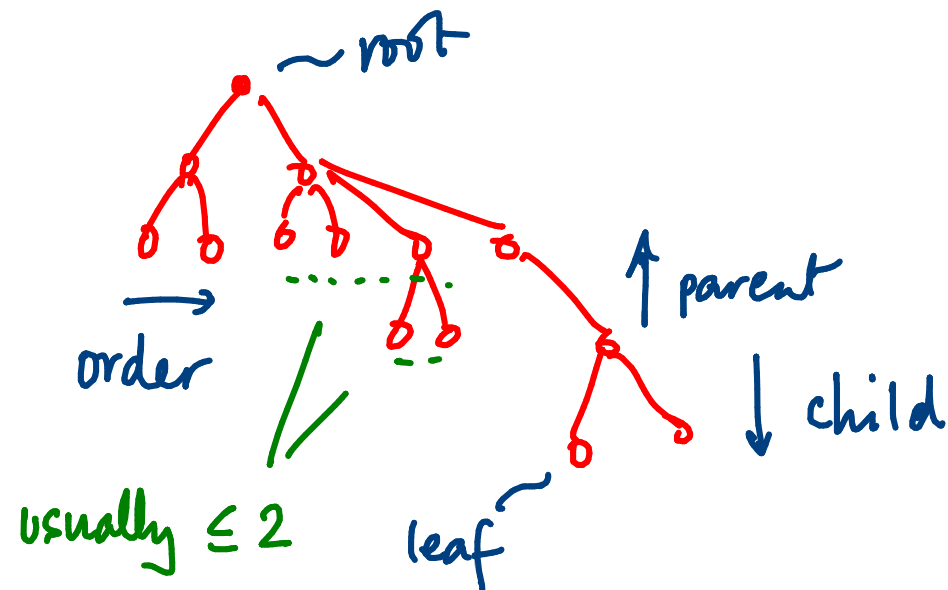
Similarity for comparisons

--eq-- , --lt-- etc

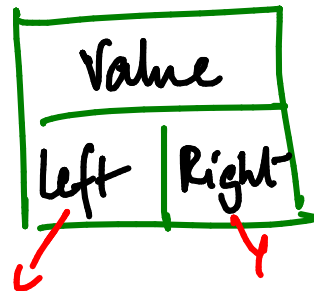
$o1 == o2$

$o1 < o2$

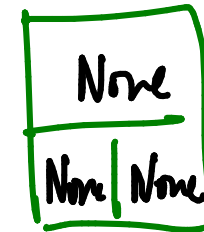
From lists to trees



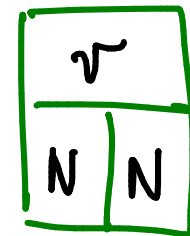
Binary Trees



Empty Tree



Leaf



class TNode:

def __init__(self, initial = None):

self.value = initial

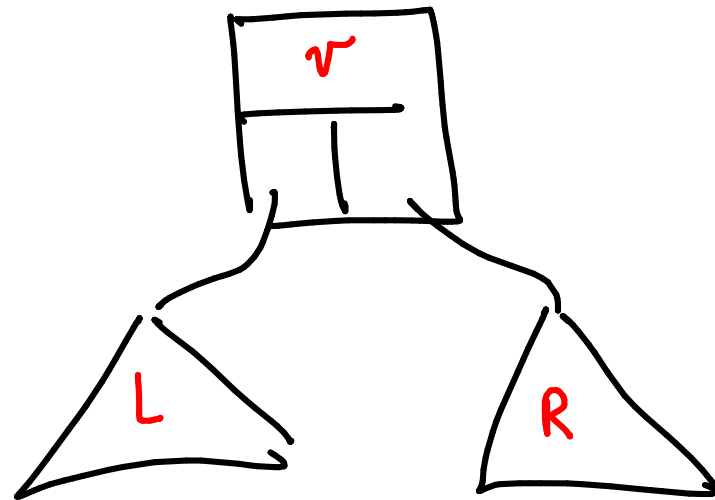
self.left = None

self.right = None

isEmpty()

isLeaf()

Search Trees (over integers)



all values in $L < v$

all values in $R > v$

No duplicate values

$\text{find}(v)$

$\text{insert}(v)$

- if $v \notin \text{tree}$, add it

$\text{delete}(v)$

- if $v \in \text{tree}$, remove it

```
def find(self, v):
```

```
    if self.isEmpty():  
        return False
```

Can also follow
path iteratively

```
    if self.value == v:  
        return True
```

↙ None is False

```
    if v < self.value and self.left:
```

```
        return self.left.find(v)
```

```
    elif v > self.value and self.right:
```

```
        return self.right.find(v)
```

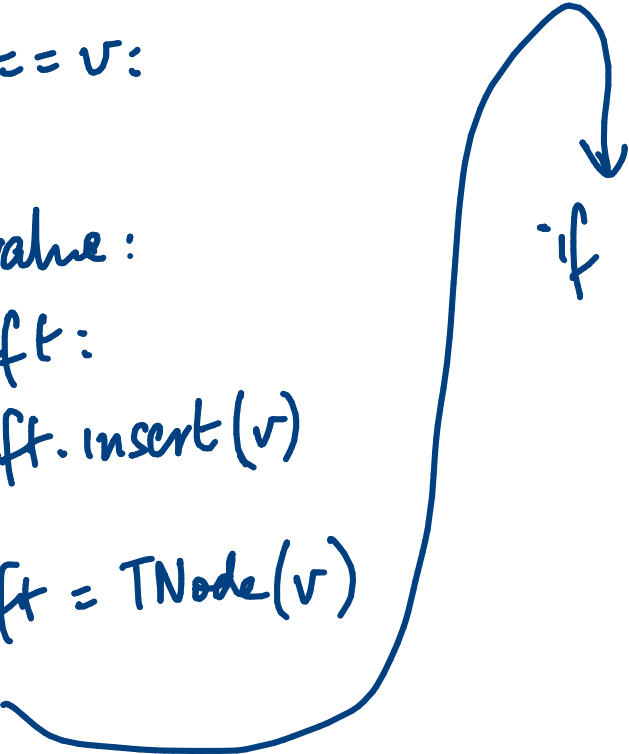
```
    else:
```

```
        return False
```



```
def insert(self, v)
    if self.isEmpty():
        self.value = v
        return
    if self.value == v:
        return
    if v < self.value:
        if self.left:
            self.left.insert(v)
        else:
            self.left = TNode(v)
    if v > self.value:
        if self.right:
            self.right.insert(v)
        else:
            self.right = TNode(v)
```

Try to find v
If False, insert at failure point



```
def delete(self, v):
```



```
def deletemax(self):
```

Locate rightmost value
in tree.

Delete it & return it

