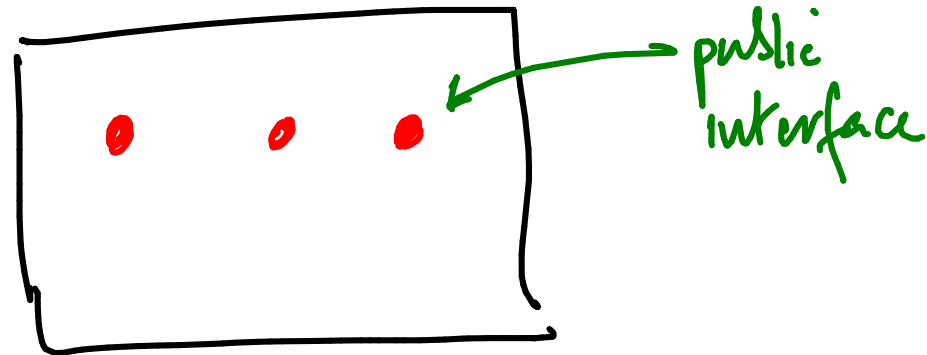
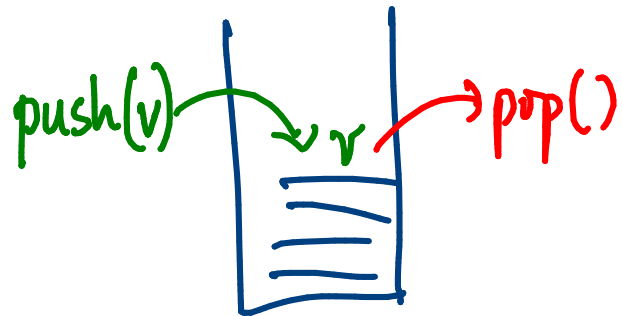


Abstract datatypes



Stack



Implement stack as list

```
def push(v):  
    l.append(v)  
def pop():  
    v = l[-1]  
    r
```

Stack as a list.

```
def push(v):
    l.append(v)
```

```
def pop():
    v = l[-1]
    del(l[-1]) ← removes last elt
    return(v)
```

Public : push(v)
pop()

Should not allow l[6] = 22 etc

Creating an abstract data type

Template - "Class"

Internal variables used to store data

How public functions update/query this internal structure

Create instances of this template "Object"

"Object Oriented Programming"

Example: Stack

```
class Stack:
    def __init__(self):
```

first arg is always self

```
    self.l = []
```

```
    def push(self, v):
```

```
        self.l.append(v)
```

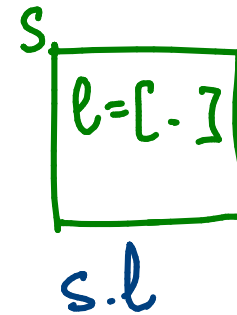
```
    def pop(self):
```

```
        v = self.l[-1]
```

```
        del(self.l[-1])
```

```
        return v
```

```
s = Stack()
```



```
push(s, v)
```

```
s.push(v)
```

Cannot rule out s.l.reverse()

Functions with optional arguments

By default, a new stack is empty

but you can initialize it at time of creation

```
def __init__(self, initial=[])  
    self.l = initial.reverse()
```

```
s = Stack()           ~ s.l is []  
s = Stack([4,3])     ~ s.l ~ [3,4]
```

Alternatively

```
def __init__(self, initial = []):
```

```
    self.l = []
```

```
    for v in initial:
```

```
        self.push(v)
```

← one function can call another

```
def isempty(self):
```

```
    return (self.l == [])
```

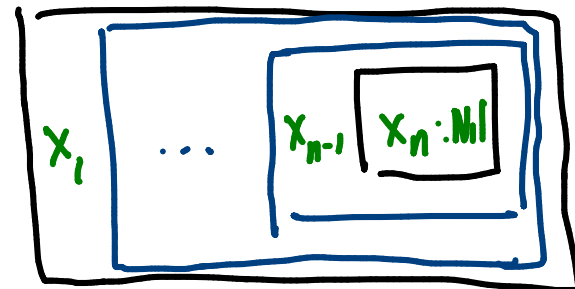
Recursive data types

A list is

- empty
- a value followed by a list

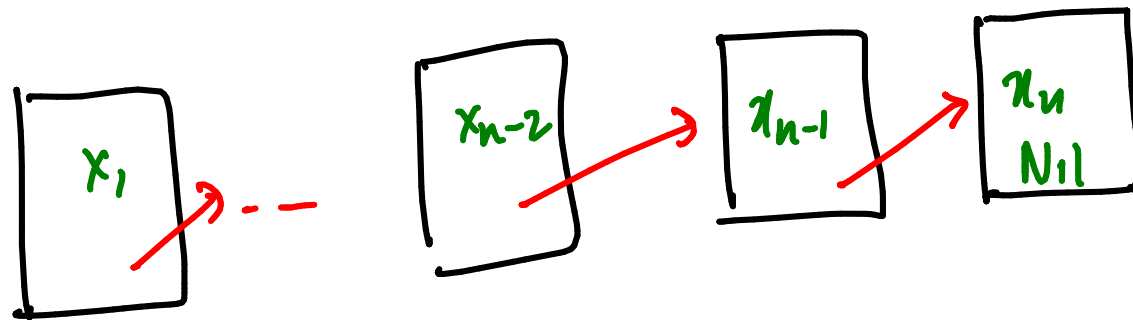
In Haskell

$$x_1 : x_2 : \dots : x_n : \text{Nil}$$

$$x_i (x_2 : \dots x_{n-1} (x_n : \text{Nil}))$$


In Python.

Pull the nested boxes apart



"Linked" list

Sequence of identical boxes

Set this up as an abstract datatype
using Class

class Node:

```
def __init__(self):
    self.value = None
    self.next = None
```

What should

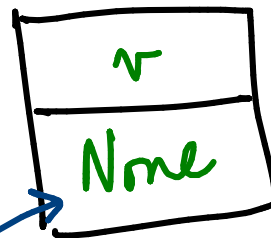
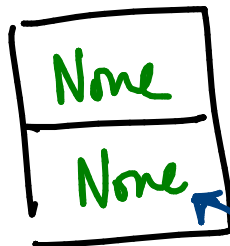
`l = Node()`
create?

-Should create
empty list

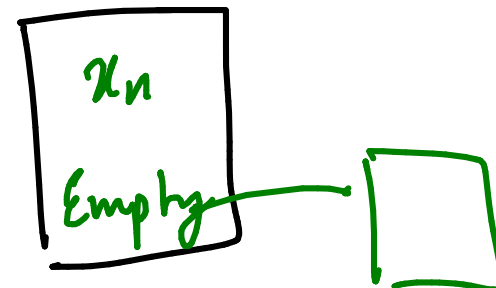
last node in list

Empty list

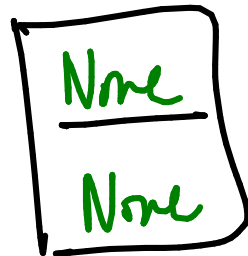
list [v]



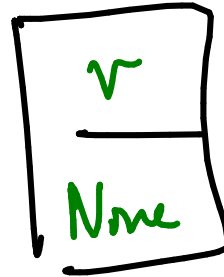
this is the last node



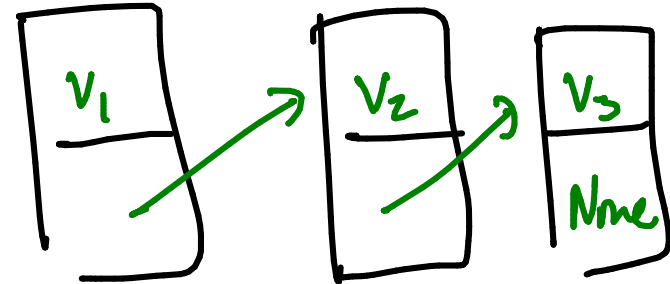
Design decision:



[]



[v]



[v₁, v₂, v₃]

Value is never None except for []

Useful to be able to create Node with or without v

class Node:

```
def __init__(self, initial = None):
```

```
    self.value = initial
```

```
    self.next = None
```

```
def isempty(self):
```

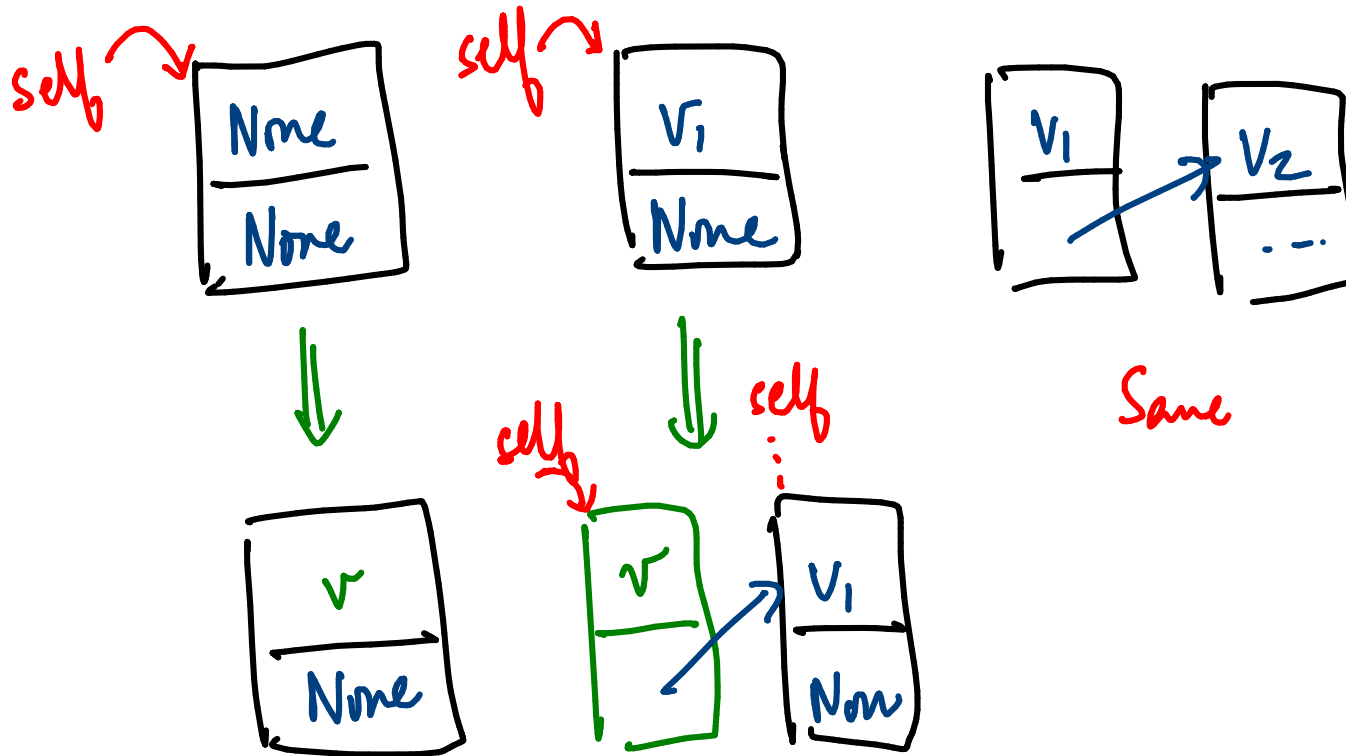
```
    return (self.value == None)
```

define

```
insert(v) - v:l
```

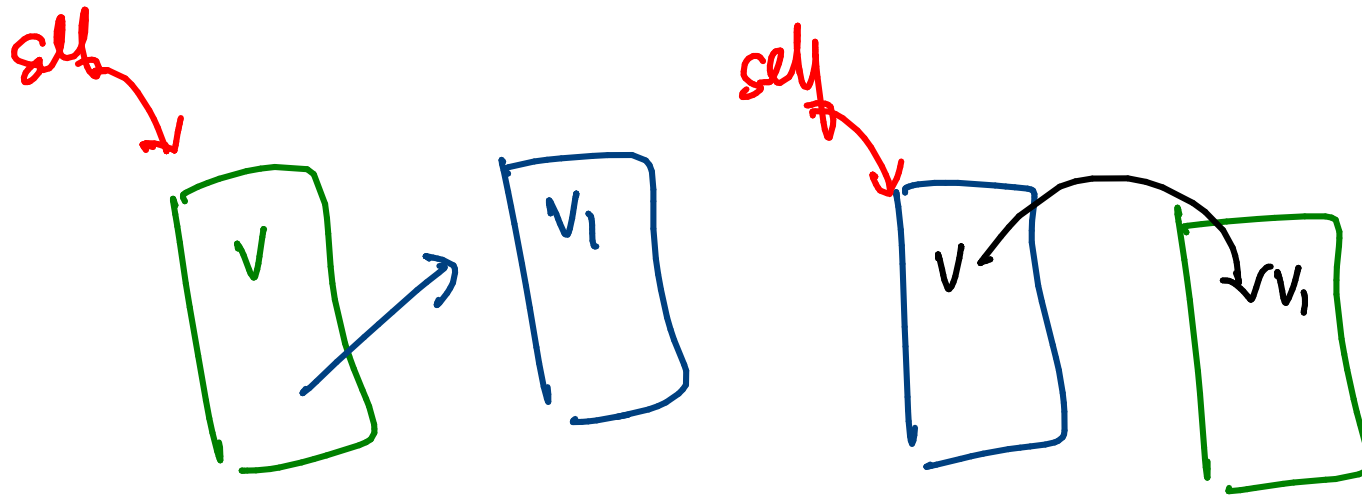
```
append(v) l.append(v)
```

Insert- v



Cannot modify what self points to inside function

Get around this?



Push new node to second position

Copy values from self to new node

Update values of self

Replumbing