

Name:

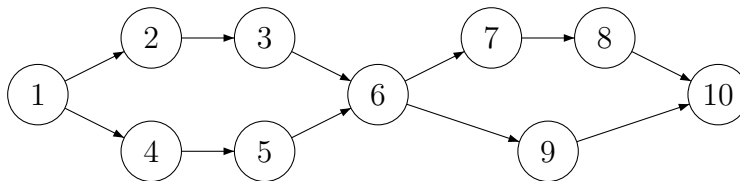
## Advanced Programming, II Semester, 2011–2012

### Quiz 4, 13 March 2012

Answer all questions in the space provided. Use the reverse for rough work, if any.

**Don't forget to fill your name!**

1. How many topological orderings does the following directed acyclic graph have?

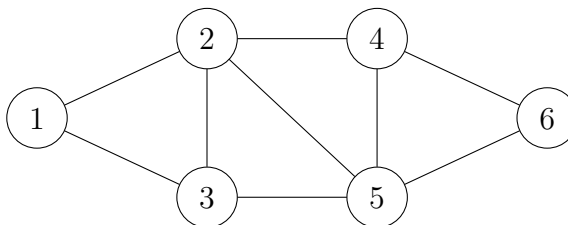


In any valid linearization, the vertices  $\{2,3,4,5\}$  must come between 1 and 6 and the vertices  $\{7,8,9\}$  must come between 6 and 10. If we fix the positions of  $\{2,3\}$ , the positions of  $\{4,5\}$  are decided. Likewise if we fix the positions of  $\{7,8\}$ , the position of 9 is decided. This gives us the following calculation for the total number of orderings.

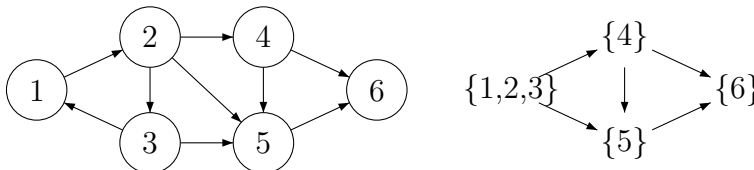
$$\binom{4}{2} \times \binom{3}{2} = 6 \times 3 = 18$$

(5 marks)

2. Orient the edges of the following undirected graph so that the resulting directed graph has *four* strongly connected components. Draw the corresponding scc dag—label each vertex of the dag with the corresponding scc.



The smallest nontrivial scc one can generate is a triangle. This means that the other three scc's must be singletons. You can orient any triangle as an scc and set up the other edges appropriately. For instance:



(5 marks)