Lecture 13: 27 Feb, 2023

Pranabendu Misra Slides by Madhavan Mukund

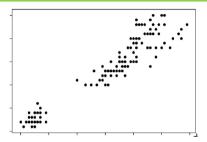
Data Mining and Machine Learning January–May 2023

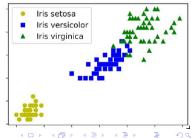
Unsupervised learning

- Supervised learning requires labelled data
- Vast majority of data is unlabelled
- What insights can you get into unlabelled data?

"If intelligence was a cake, unsupervised learning would be the cake, supervised learning would be the icing on the cake

- Yann LeCun ACM Turing Award 2018







Applications

- Customer segmentation
 - Marketing campaigns
- Anomaly detection
 - Outliers
- Semi-supervised learning
 - · Propagate limited labels
- Image segmentation
 - · Object detection



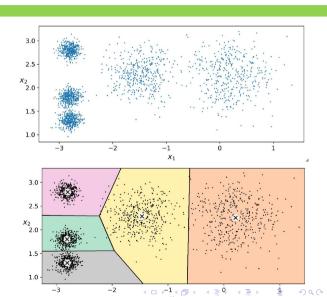




Clustering

- Find natural groups of data
- Define a distance measure
- Group together data that is close together
- Top down
 - · Partition data into clusters
- Bottom up
 - · Group items into clusters



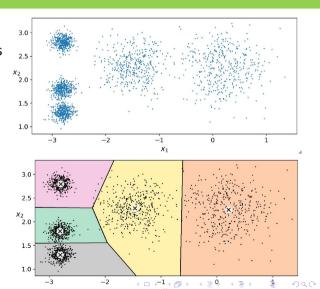


Top down clustering

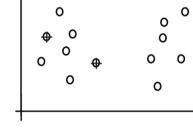
K Means Clustering

- Data items are points in n dimensions
 - $(x_1, x_2, ..., x_n)$
- Partition into K clusters
 - Fix K in advance
- Each cluster is represented by its geometric centre
 - Centroid, or mean
 - Hence "K means"





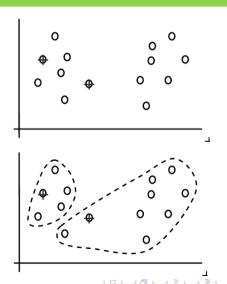
- Choose K points initially as random centroids
- In each iteration
 - Assign each point to nearest centroid
 - Recompute centroids
- Termination
 - Clusters stabilize
 - Sum square distance is below threshold





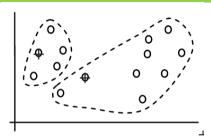
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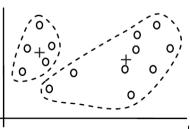




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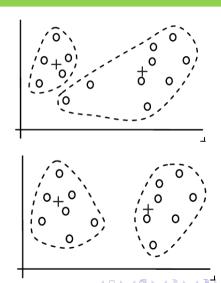






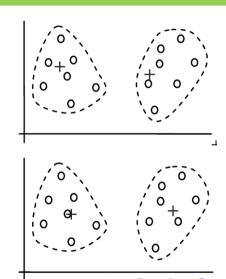
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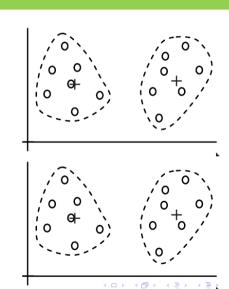
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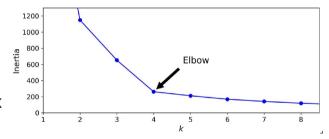


Evaluating clustering

- How "tight" are the clusters?
- Mean squared distance from centroids inertia

$$\frac{1}{n} \sum_{j=1}^{K} \sum_{x \in C_j} dist(x, centroid_j)^2$$

- Plot inertia for different values of K and look for optimum
- Can also use change in inertia threshold to stop iterations



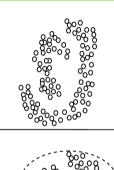


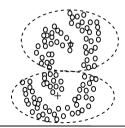
Advantages

- Efficient each iteration makes a single pass over data
 - · Incrementally compute centroid

Disadvantages

Can only find clusters that look like ellipses







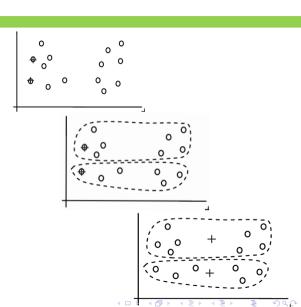


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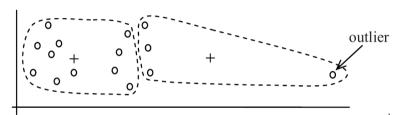
Disadvantages

- Can only find clusters that look like ellipses
- Choice of initial random centroid matters
 - Repeat and check



Outliers

- Anomalous values
 - Far away from all centroids
- But clustering with outliers distorts clusters
- How to identify outliers before clustering?





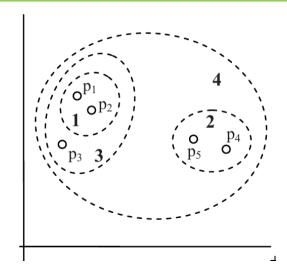


Clustering

- K Means clustering can only find clusters that look like ellipses
- Instead, build clusters bottom up, by merging clusters

Hierarchical clustering

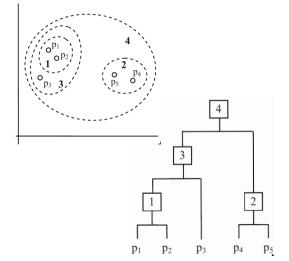
- Initially, each item is a singleton cluster
- At each step, merge nearest clusters





Hierarchical Clustering

- Initially, each item is a singleton cluster
- At each step, merge nearest clusters
- Can represent process using a tree dendrogram
- Choose appropriate level in dendrogram for final clustering





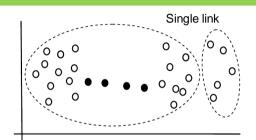


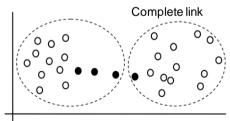
Hierarchical Clustering

To merge clusters, define distance between clusters

- Single link: distance between closest points
 - Creates chain effect
- Complete link: maximum of pairwise distances
- Average link: mean of pairwise distances
- All require O(n²) computation expensive

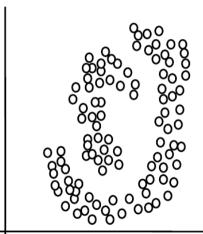






Clustering

- How to identify odd shaped clusters?
- Cluster group of points that are "close together"
- Identify "dense" neighbourhoods
- How do we formalize this?

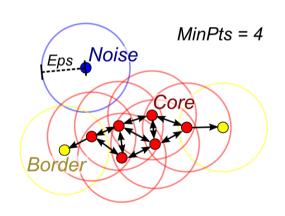




Density based clustering

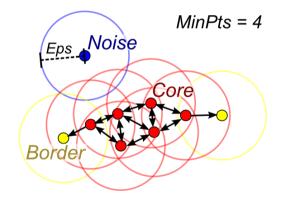
- Construct a small ball around each point, radius Eps
- Identify a threshold for neighbours within ball, MinPts
- Core point has at least MinPts neighbours inside Eps ball
- Connect each core point to all its neighbours
- Border points attached to core points but not core themselves
- Noise disconnected points





Density based clustering

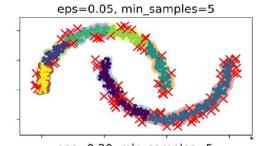
- Formally, edges from core points to neighbours define a directed graph
- Border points are part of this graph, but cannot add edges to extend the graph
- Discard the edge directions
- Connected components are clusters

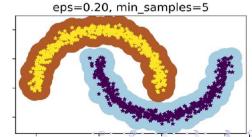




Dbscan

- Implementation of density based clustering available in Python and R
- Smaller value of Eps subdivides into small clusters
- Larger *Eps* groups larger clusters



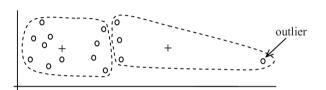


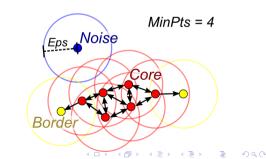


Outliers and clustering

- Outliers are points that lie outside natural clusters
- K Means far away from all centroids
 - But outliers can distort the clustering process
- Density based clustering not connected to any core point
 - But density is applied uniformly

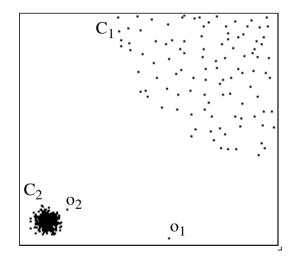






Outliers and density

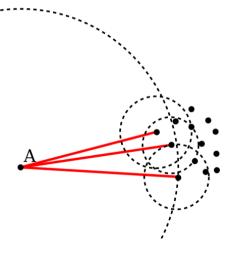
- An outlier is less dense than its nearest neighbours
- But difference in density may be local
- A distance metric to eliminate o₂ could make all of C₁ outliers
- C₁ has 400 points, C₂ has 100 points
- Larger distance would make all of C₂ outliers with respect to C₁





Outliers and density

- For clustering, we defined a radius Eps and looked for MinPts neighbours within that ball
- Instead, fix MinPts and find smallest ball with that many neighbours
- Compare radius(p) with radius of its neighours
- A is an outlier because its radius is much more than that of its neighbours





Outliers and density

Local outlier factor LOF(p)

 $\frac{\text{Mean radius of } \textit{MinPts-neighbours}(p)}{radius(p)}$

- The smaller this ratio, the more likely that *p* is an outlier
- Comparison is local to neighbourhood, so this can deal with different densities across range of data

