#### Data Mining and Machine Learning

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### Limitations of classification models

- Bias : Expressiveness of model limits classification
  - ► For instance, linear separators
- Variance: Variation in model based on sample of training data
  - Shape of a decision tree varies with distribution of training inputs

Models with high variance are expressive but unstable

- In principle, a decision tree can capture an arbitrarily complex classification criterion
- Actual structure of the tree depends on impurity calculation
- Danger of overfitting: model tied too closely to training set
- Is there an alternative to pruning?

### Ensemble models

- Sequence of independent training data sets  $D_1$ ,  $D_2$ , ...,  $D_k$
- Generate models  $M_1$ ,  $M_2$ , ...,  $M_k$
- Take this ensemble of models and "average" them
  - For regression, take the mean of the predictions
  - For classification, take a vote among the results and choose the most popular one
- Challenge: Infeasible to get large number of independent training samples
- Can we build independent models from a single training data set?
  - Strategy to build the model is fixed
  - Same data will produce same model

# Bootstrap Aggregating = Bagging

- Training data has N items
  - $TD = \{d_1, d_2, \ldots, d_N\}$
- Pick a random sample with replacement
  - Pick an item at random (probability  $\frac{1}{N}$ )
  - Put it back into the set
  - Repeat K times
- Some items in the sample will be repeated
- If sample size is same as data size (K = N), expected number of distinct items is  $(1 \frac{1}{e}) \cdot N$ 
  - Approx 63.2%

# Bootstrap Aggregating = Bagging

- Sample with replacement of size N : bootstrap sample
  - Approx 2/3 of full training data
- Take k such samples
- Build a model for each sample
  - Models will vary because each uses different training data
- Final classifier: report the majority answer
  - Assumptions: binary classifier, *k* odd
- Provably reduces variance



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### When to use bagging

- Bagging improves performance when there is high variance
  - Independent samples produce sufficiently different models
- A model with low variance will not show improvement
  - k-nearest neighbour classifier
  - ▶ Given an unknown input, find *k* nearest neighbours and choose majority
  - Across different subsets of training data, variation in k nearest neighbours is relatively small
  - Bootstrap samples will produce similar models

#### Random Forest

- Applying bagging to decision trees with a further twist
- As before, k bootstrap samples  $D_1, D_2, \ldots, D_k$
- For each  $D_i$ , build decision tree  $T_i$  as follows
  - Each data item has M attributes
  - ► Normally, choose maximum impurity gain among *M* attributes, then best among remaining *M* − 1, ...
  - Instead, fix a small limit m < M say  $m = \log_2 M + 1$
  - At each level, choose a random subset of available attributes of size m
  - Evaluate only these m attributes to choose next query
  - No pruning build each tree to the maximum
- Final classifier: vote on the results returned by  $T_1$ ,  $T_2$ , ...,  $T_k$

### Random Forest ...

- Theoretically, overall error rate depends on two factors
  - Correlation between pairs of trees higher correlation results in higher overall error rate
  - Strength (accuracy) of each tree higher strength of individual trees results in lower overall error rate
- Reducing *m*, the number of attributes examined at each level, reduces correlation and strength
  - Both changes influence the error rate in opposite directions
- Increasing *m* increases both correlation and strength
- Search for a value of *m* that optimizes overall error rate

# Out of bag error estimate

- Each bootstrap sample omits about 1/3 of the data items
- Hence, each data item is omitted by about 1/3 of the samples
- If data item d does not appear in bootstrap sample D<sub>i</sub>, d is out of bag (oob) for D<sub>i</sub>
- Oob classification for each d, vote only among those T<sub>i</sub> where d is oob for D<sub>i</sub>
- Oob samples serve as a test data set
  - Estimate generalization error rate of overall model based on error rate of oob classification without a separate test data set
- Can also estimate relative significance of attributes
  - ▶ For a given tree, perturb the values of attribute *A* in oob data items
  - Measure the change in error rate for oob samples