

---

---

---

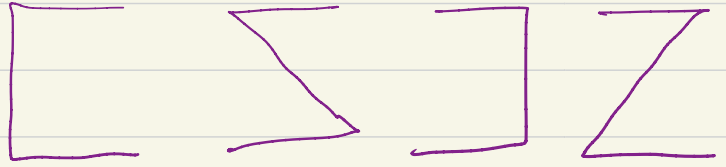
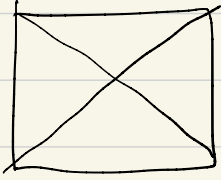
---

---









# Lecture - 1

- SETS & FUNCTIONS. notation.
- Constructing numbers in base  $b$ ;
- Induction ..... Boolean connectives;

PI:

$\mathcal{U} = \text{universe}$

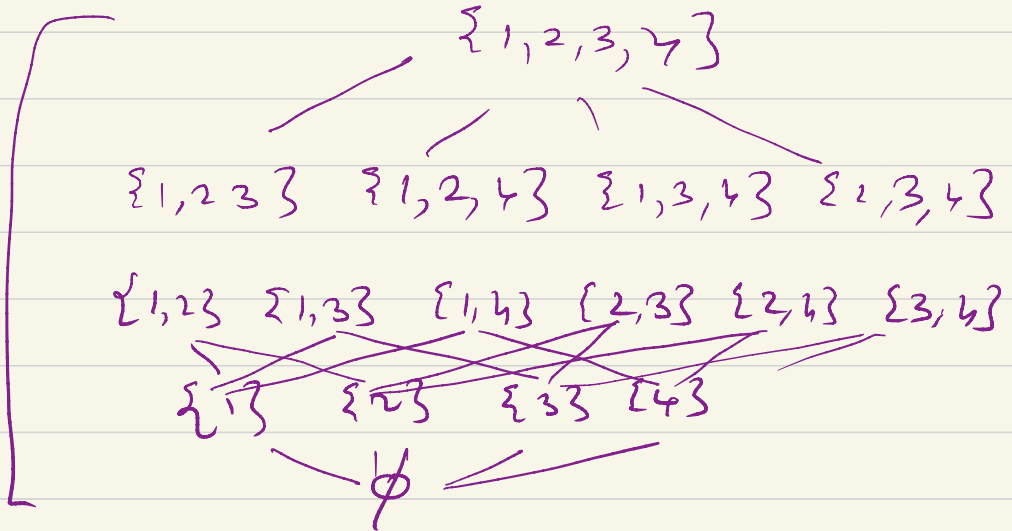
$\{x_1, \dots, x_n\}$ .

$\emptyset \quad \{\emptyset\}$

$\mathcal{U} = \{1, 2, 3, 4\}$ .

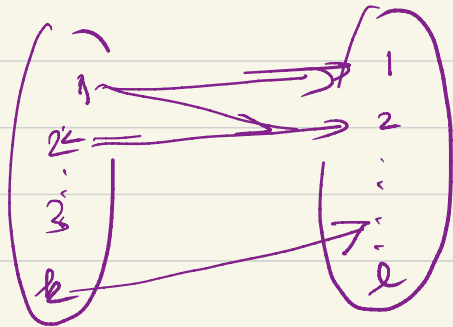
$A \subseteq B$

$A \subsetneq B$



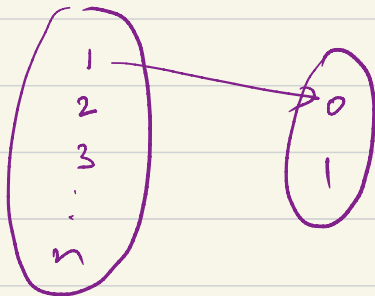
$$f: S_1 \rightarrow S_2$$

$$S_1 = \{1, \dots, k\} \quad S_2 = \{1, \dots, l\}$$

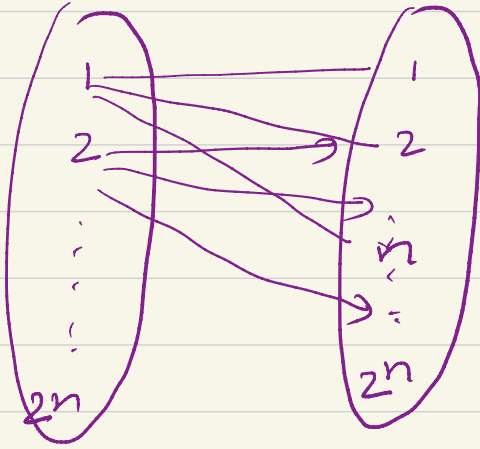


Relation:

$$\{(1,1), (1,2), (2,2), (3,3), \dots, (k,k)\}$$



$2^n$  functions



$$(2^n)^n$$

$$2^{n \cdot n}$$

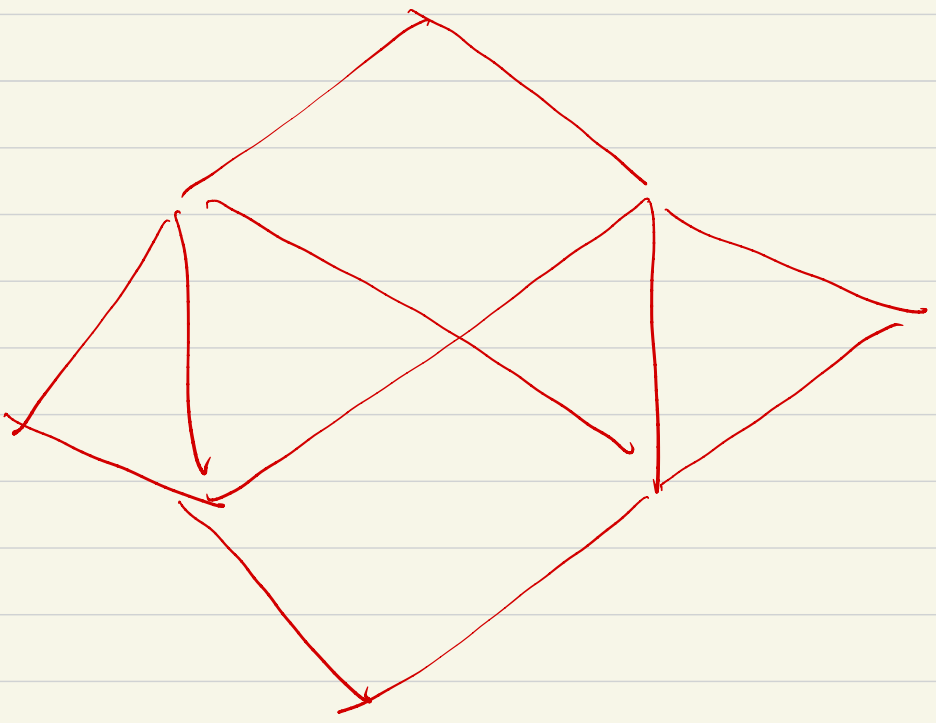
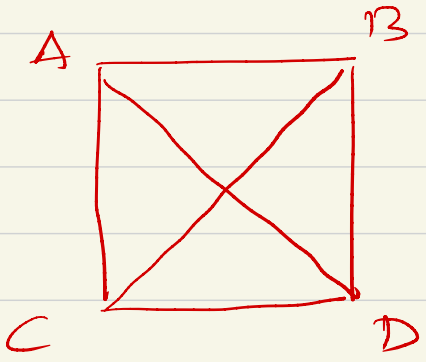
How many <sup>bijjective</sup> functions from this relation?

Write a program! # operations?

[ WE DO NOT KNOW OF A PROGRAM WHICH TAKES SUBEXPONENTIAL # steps ]

↪ in the size of the input.





$x_1, \dots, x_n.$

$$x_i \in \{0, 1\};$$

$$(x_i \vee x_j) = \max \{x_i, x_j\}$$

$$(x_i \wedge x_j) = \min \{x_i, x_j\}.$$

$$\neg x_i \stackrel{\Delta}{=} \bar{x}_i$$

---

$$(x_1 \vee \bar{x}_2 \vee x_3) \wedge (x_1 \vee x_4 \vee x_6) \wedge$$

$$(x_7 \vee x_8 \vee x_9) \wedge (\bar{x}_2 \vee \bar{x}_4 \vee x_{10}) \wedge$$

- - -

Q: Is there an assignment of values to  $x_1, \dots, x_n$  which makes the expression True.

—  $x$  —  $x$  —  $x$  —

PROGRAM.<sup>2</sup>

Again, we only know of a brute force solution. Nothing better than exponential in

$n, m$   
↑ ↘ # clauses.

# literals

This is believed to be easier than <sup>finding</sup> # bijections in relations.