

Rough list of topics for Quantum Mechanics 1, CMI Spring 2011.

1. Introductory remarks: why quantum theory?  $\langle 1 \rangle$
2. Review of classical mechanics  $\langle 3 \rangle$ 
  - (a) Newton's equation
  - (b) Generalized coordinates, degrees of freedom,
  - (c) Energy, Hamiltonian, momentum, angular momentum
  - (d) Hamilton's equations
  - (e) Conserved quantities
  - (f) Action principle and Lagrangian formulation
3. Basic concepts of waves  $\langle 3 \rangle$ 
  - (a) Traveling, standing, sinusoidal, monochromatic, plane and spherical waves
  - (b) Amplitude, wave number, frequency, wave vector and intensity
  - (c) Wave equations
  - (d) Wave packets and width of wave packet
  - (e) Dispersive waves, group velocity of wave packet
4. Experimental basis & historical development of quantum mechanics
  - (a) Quanta of light/radiation  $\langle 3 \rangle$ 
    - i. Black body radiation & Planck hypothesis
    - ii. Photoelectric effect
    - iii. Compton effect
  - (b) Wave and quantum properties of matter  $\langle 5 \rangle$ 
    - i. Discrete atomic spectra and stability of the atom
    - ii. Bohr Model of the atom
    - iii. Franck-Hertz experiment
    - iv. Raman scattering and discrete molecular spectra
    - v. de Broglie hypothesis on matter waves
    - vi. Electron diffraction: Davisson, Germer & Thompson experiment
    - vii. Double slit interference experiment: wave function as a probability amplitude
    - viii. Wave-particle duality and complementarity principle
5. Schrödinger equation, postulates and formulation of quantum mechanics  $\langle 7 \rangle$ 
  - (a) Schrödinger equation from de Broglie matter wave hypothesis  $\langle \frac{1}{2} \rangle$
  - (b) Wavefunction, probability density and current  $\langle \frac{1}{2} \rangle$
  - (c) Superposition principle and vector space of states  $\langle \frac{1}{2} \rangle$
  - (d) Dirac Delta function  $\langle \frac{1}{2} \rangle$

- (e) Expectation values of observables in a state  $\langle \frac{1}{2} \rangle$
  - (f) Ehrenfest's theorem  $\langle \frac{1}{2} \rangle$
  - (g) Hilbert space of quantum states, Dirac bra-ket notation  $\langle 1 \rangle$
  - (h) Position eigenstates  $\langle \frac{1}{3} \rangle$
  - (i) Momentum eigenstates  $\langle \frac{1}{3} \rangle$
  - (j) Relation between  $\hat{x}$  and  $\hat{p}$ : Heisenberg commutation relation and uncertainty  $\langle \frac{1}{3} \rangle$
  - (k) Hermiticity of observables  $\langle \frac{1}{2} \rangle$
  - (l) Collapse of the wavefunction/measurement and probability postulate  $\langle \frac{1}{4} \rangle$
  - (m) Summary of postulates of quantum mechanics  $\langle \frac{1}{4} \rangle$
  - (n) Energy eigenstates: Time-independent Schrödinger equation  $\langle \frac{1}{2} \rangle$
  - (o) Time evolution operator  $\langle \frac{1}{2} \rangle$
6. One dimensional quantum mechanical models  $\langle 8 \rangle$
- (a) Particle in an infinite square well  $\langle 1.5 \rangle$
  - (b) Free particle  $\langle 2 \rangle$ 
    - i. plane waves
    - ii. minimal uncertainty gaussian wave packet
  - (c) Harmonic oscillator  $\langle 4.5 \rangle$ 
    - i. Variational approach
    - ii. Algebraic approach: creation and annihilation operators
    - iii. Analytic approach: Hermite polynomials
7. Some general properties of 1 dimensional quantum systems  $\langle 3 \rangle$
- (a) Parity  $\langle \frac{1}{2} \rangle$
  - (b) Time development of expectation values  $\langle \frac{1}{4} \rangle$
  - (c) Symmetries and conserved quantities: parity, space and time translations  $\langle \frac{1}{2} \rangle$
  - (d) Energy-time uncertainty relation  $\langle \frac{1}{4} \rangle$
  - (e) Absence of degenerate bound states in 1d  $\langle \frac{1}{2} \rangle$
  - (f) Schrödinger vs Heisenberg pictures & equations of motion  $\langle \frac{1}{2} \rangle$
  - (g) Complete sets of commuting observables  $\langle \frac{1}{2} \rangle$
8. Models with bound and scattering states in 1 dimension; Tunneling  $\langle 3 \rangle$
- (a) Delta function potential: bound states  $\langle \frac{1}{2} \rangle$
  - (b) Reflection and Transmission coefficients  $\langle \frac{1}{2} \rangle$
  - (c) Scattering against a delta function potential  $\langle \frac{1}{2} \rangle$
  - (d) Bound states of finite square well  $\langle 1 \rangle$
  - (e) Scattering against a rectangular barrier  $\langle \frac{1}{2} \rangle$

9. Simple problems in two dimensions  $\langle 1 \rangle$

- (a) Free particle in two-dimensions
- (b) Two dimensional infinite square well
- (c) Parity in two dimensions
- (d) Two dimensional harmonic oscillator

10. Quantum mechanics in 3d: Central potentials  $\langle 5 \rangle$

- (a) Free particle in Cartesian coordinates, hamiltonian in polar coordinates  $\langle \frac{1}{3} \rangle$
- (b) Basic properties of angular momentum  $\langle \frac{2}{3} \rangle$
- (c) Angular momentum and rotations  $\langle \frac{1}{3} \rangle$
- (d) Free particle in spherical coordinates, radial momentum  $\langle \frac{1}{3} \rangle$
- (e) Hermiticity and positivity of free particle hamiltonian  $\langle \frac{1}{3} \rangle$
- (f) Conservation of angular momentum in a central potential  $\langle \frac{1}{3} \rangle$
- (g) Separation of variables for particle in central potential  $\langle \frac{1}{3} \rangle$
- (h) Preview of spectrum of angular momentum  $L^2, L_z$ .  $\langle \frac{1}{3} \rangle$
- (i) Free particle radial eigenfunctions.  $\langle \frac{1}{2} \rangle$
- (j) Particle in a spherical well.  $\langle \frac{1}{2} \rangle$
- (k) Joint spectrum of  $L^2$  and  $L_z$ : spherical harmonics  $\langle \frac{1}{3} \rangle$
- (l) Eigenvalues of  $L^2$  and  $L_z$  by ladder operators  $\langle \frac{1}{3} \rangle$
- (m) Spectrum of Hydrogen atom, radial eigenfunctions  $\langle \frac{1}{3} \rangle$