

# Unit-3: Linear-time properties

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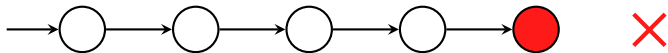
Chennai Mathematical Institute

*NPTEL-course*

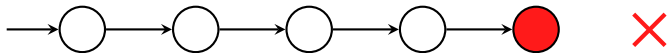
July - November 2015

Module 5:  
**Liveness properties**

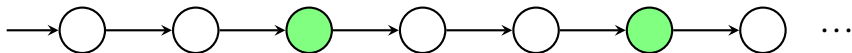
**Safety:** Something bad **never** happens



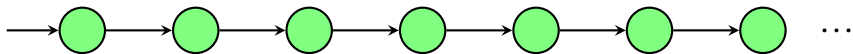
**Safety:** Something bad **never** happens



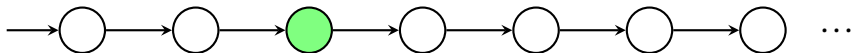
**Liveness:** Something **good** happens **infinitely often**



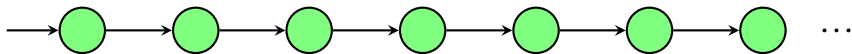
$G p$ : Always  $p$



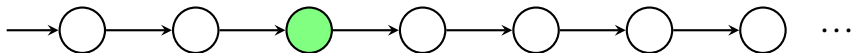
$F p$ : Sometime  $p$



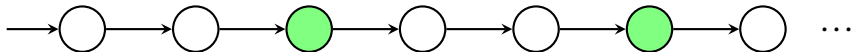
$G p$ : Always  $p$



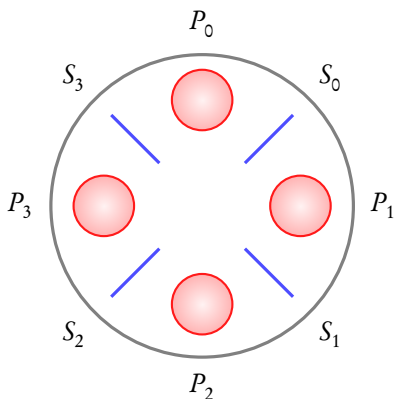
$F p$ : Sometime  $p$



$G F p$ : Infinitely often  $p$



# Recall...



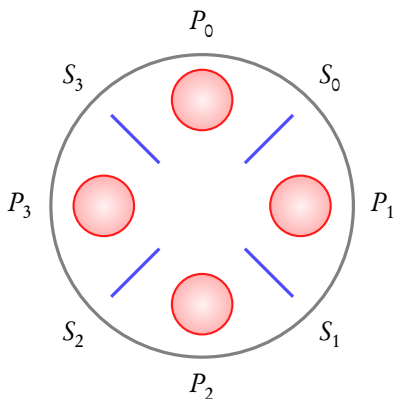
$P_0 \dots P_3$ : *philosophers*

$S_0 \dots S_3$ : *chop-sticks*

**Philosopher  $P_i$  can eat**  
only if  
he has access to **chop-sticks**

$S_{(i-1) \bmod 4}$  and  $S_{i \bmod 4}$

# Recall...



$P_0 \dots P_3$ : *philosophers*

$S_0 \dots S_3$ : *chop-sticks*

**Philosopher  $P_i$  can eat**

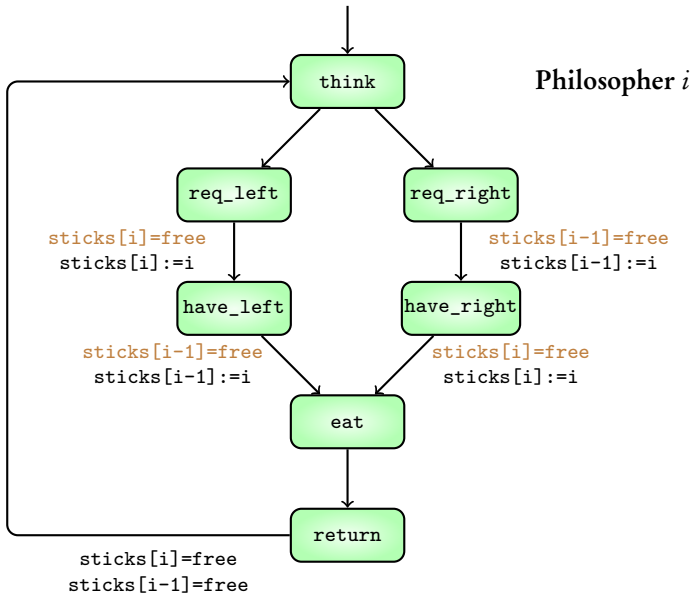
only if

he has access to **chop-sticks**

$S_{(i-1) \bmod 4}$  and  $S_{i \bmod 4}$

What should the **protocol** be so that **every philosopher** can eat **infinitely often**?





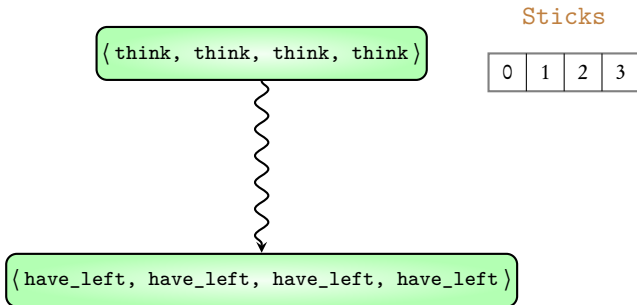
NuSMV code for the protocol

## Sticks

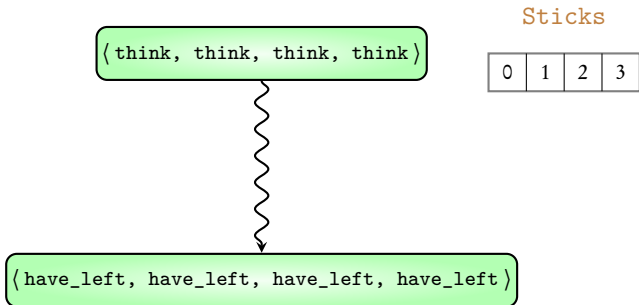
`< think, think, think, think >`

|   |   |   |   |
|---|---|---|---|
| 0 | 1 | 2 | 3 |
|---|---|---|---|

`< have_left, have_left, have_left, have_left >`



What properties should be checked in order to **reveal the deadlock?**



What properties should be checked in order to **reveal the deadlock**?

`G F (phil0.location=eat) & G F (phil1.location=eat) &`  
`G F (phil2.location=eat) & G F (phil3.location=eat)`

- ▶ If **counterexample** is due to only main process being scheduled
  - ▶ **Not a fair** scheduler

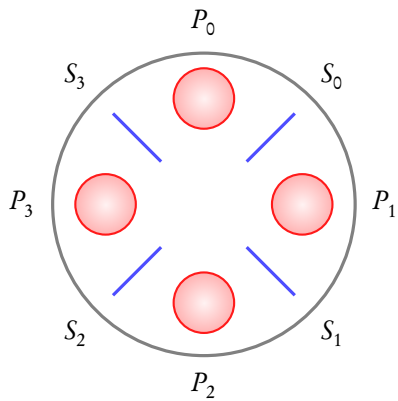
- ▶ If **counterexample** is due to only main process being scheduled
  - ▶ **Not a fair** scheduler
  - ▶ Add a **FAIRNESS** running in the philosopher module

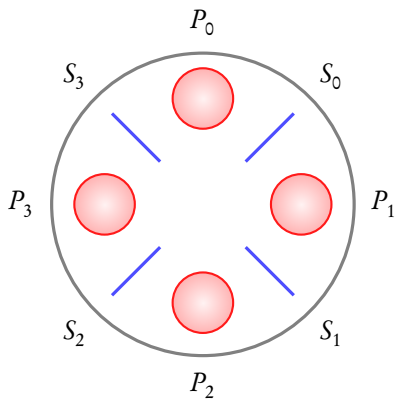
- ▶ If **counterexample** is due to only main process being scheduled
  - ▶ **Not a fair** scheduler
  - ▶ Add a **FAIRNESS** running in the philosopher module

NuSMV demo

Coming next: Another solution for the dining philosophers problem

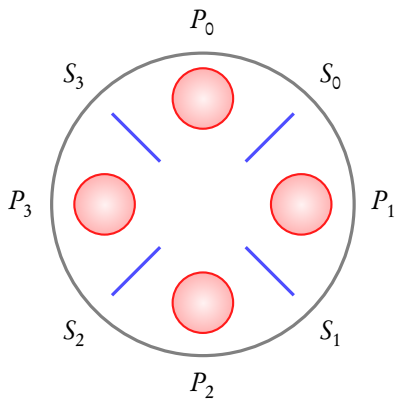






Sticks

|   |   |   |   |
|---|---|---|---|
| 0 | 2 | 2 | 0 |
|---|---|---|---|

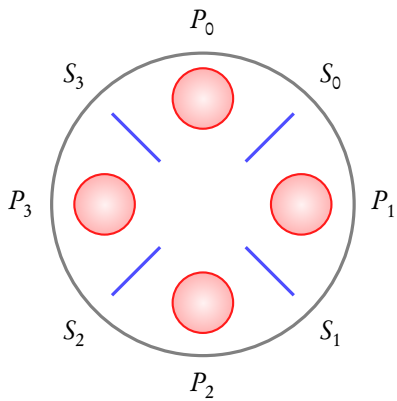


Sticks

|   |   |   |   |
|---|---|---|---|
| 0 | 2 | 2 | 0 |
|---|---|---|---|



|   |   |   |   |
|---|---|---|---|
| 1 | 1 | 3 | 3 |
|---|---|---|---|



Sticks

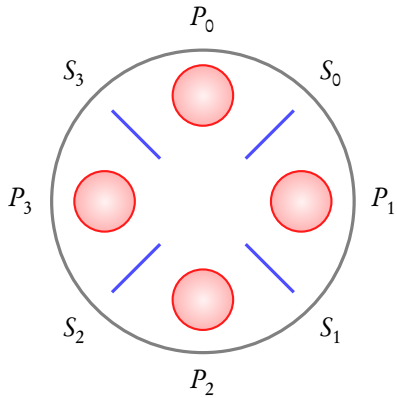
|   |   |   |   |
|---|---|---|---|
| 0 | 2 | 2 | 0 |
|---|---|---|---|



|   |   |   |   |
|---|---|---|---|
| 1 | 1 | 3 | 3 |
|---|---|---|---|



|   |   |   |   |
|---|---|---|---|
| 0 | 2 | 2 | 0 |
|---|---|---|---|



Sticks

|   |   |   |   |
|---|---|---|---|
| 0 | 2 | 2 | 0 |
|---|---|---|---|



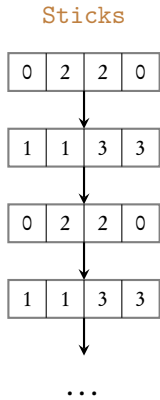
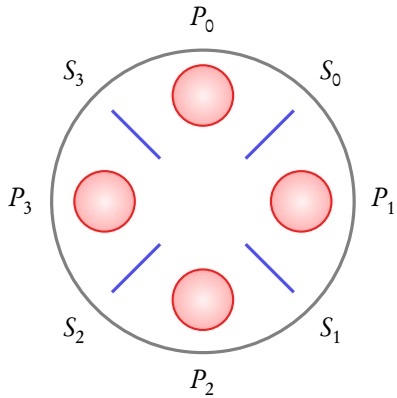
|   |   |   |   |
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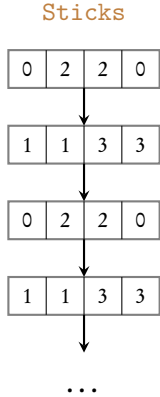
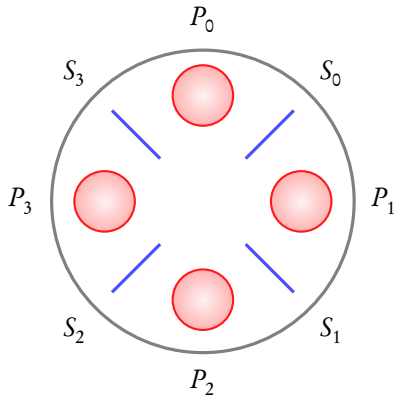


|   |   |   |   |
|---|---|---|---|
| 0 | 2 | 2 | 0 |
|---|---|---|---|



|   |   |   |   |
|---|---|---|---|
| 1 | 1 | 3 | 3 |
|---|---|---|---|





This solution is deadlock-free

## Liveness properties

Good happens **infinitely often**

FAIRNESS running